

1 **Effects of Rotation on the Multi-Scale Organization of Convection in a**
2 **Global 2-D Cloud-Resolving Model**

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ABSTRACT

16 Atmospheric convection exhibits distinct spatio-temporal variability at dif-
17 ferent latitudes. A good understanding of the effects of rotation on the multi-
18 scale organization of convection from mesoscale to synoptic scale to plane-
19 tary scale is still lacking. Here cloud-resolving simulations with fixed sur-
20 face fluxes and radiative cooling are implemented with constant rotation in
21 a two-dimensional (2-D) planetary domain to simulate multi-scale organiza-
22 tion of convection from the tropics to mid-latitudes. All scenarios are divided
23 into three rotation regimes (weak, order-one, and strong) to represent ide-
24 alized ITCZ region ($0^\circ \sim 6^\circ$ N), Indian monsoon region ($6^\circ \sim 20^\circ$ N), and
25 mid-latitude region ($20^\circ \sim 45^\circ$ N), respectively. In each rotation regime, a
26 multi-scale asymptotic model is derived systematically and used as a diag-
27 nistic framework for energy budget analysis. The results show that planetary-
28 scale organization of convection only arises in the weak rotation regime, while
29 synoptic-scale organization dominates (vanishes) in the order-one (strong) ro-
30 tation regime. The depletion of planetary-scale organization of convection
31 as the magnitude of rotation increases is attributed to the reduced planetary
32 kinetic energy of zonal winds, mainly due to the decreasing acceleration ef-
33 fect by eddy zonal momentum transfer from mesoscale convective systems
34 (MCSs) and increasing deceleration effect by the Coriolis force. Similarly, the
35 maintenance of synoptic-scale organization is related to the acceleration effect
36 by MCSs. Such decreasing acceleration effects by MCSs on both planetary
37 and synoptic scales are further attributed to less favorable conditions for con-
38 vection provided by background sounding of low-level equivalent potential
39 temperature and vertical shear of zonal winds, resulting from the increasing
40 magnitude of rotation.

41 **1. Introduction**

42 Atmospheric convection plays a crucial role in the horizontal and vertical transport of mo-
43 mentum, heat, and moisture of large-scale circulation on the earth (Schneider 2006). After
44 decades of observational studies based on satellite and in situ measurements, it is apparent now
45 that the spatio-temporal variability of convection has distinct characteristics at different latitudes
46 (Riemann-Campe et al. 2009). Specifically, tropical convection is organized in a hierarchy of
47 spatio-temporal scales, ranging from a cumulus cloud of several kilometers and a few minutes to
48 MCSs (Houze 2004) of several hundred kilometers and a few hours to convective coupled equa-
49 torial waves (CCEWs) (Kiladis et al. 2009) of thousand kilometers and 1-2 weeks to the Madden-
50 Julian oscillations (MJOs) (Zhang 2005) of ten thousand kilometers and 1-3 months. In contrast,
51 convection in the subtropics is dominated by synoptic-scale convective disturbances such as low
52 pressure systems in the Indian monsoon trough region (Hurley and Boos 2015). Theoretically, the
53 magnitude of rotation can dramatically influence the behavior of geophysical flows (Majda 2000).
54 In the mid-latitudes, the strong rotation leads to a strict temporal frequency scale separation be-
55 tween potential vorticity dynamics and fast gravity waves. In contrast, the weak rotation in the
56 tropics does not induce a time scale separation any more but allows multi-scale organization of
57 convection in the presence of warm surface temperature and abundant moisture (Majda 2012).

58 Contemporary global climate models (GCMs) struggle to accurately simulate the multi-scale
59 organization of tropical convection. In fact, present-day GCMs still have difficulty in simulating
60 key features of propagating MJOs (Jiang et al. 2015), although predictions of the MJO have im-
61 proved over the past decade (Kim et al. 2018). Furthermore, it is observed that the MJO is a slowly
62 eastward-moving planetary-scale envelope that contains a few superclusters of cloudiness with nu-
63 merous embedded cloud clusters (Nakazawa 1988; Chen et al. 1996). Even good GCMs fail to

⁶⁴ satisfactorily simulate these multi-scale features (Guo et al. 2015). It is hypothesized here that the
⁶⁵ poorly simulated MJOs in the GCMs is due to an inadequate treatment of multi-scale interactions
⁶⁶ of convection, especially the upscale impact of organized tropical convection such as MCSs that
⁶⁷ are poorly resolved in the coarse-resolution GCM simulations.

⁶⁸ To address this issue, it is necessary to obtain a better understanding of spatio-temporal scale
⁶⁹ selection and multi-scale interactions of convection. With the development of computational re-
⁷⁰ source, cloud-resolving models (CRMs) have become a practically useful tool for simulating or-
⁷¹ ganized convection in a fine horizontal resolution of a few kilometers (Khairoutdinov and Randall
⁷² 2003; Miura et al. 2007; Tao and Moncrieff 2009; Guichard and Couvreux 2017). In particular,
⁷³ the 2-D CRM simulations provide a cheap way to study the multi-scale organization of convec-
⁷⁴ tion in a planetary domain. For example, the idealized 2-D CRM simulation by Grabowski and
⁷⁵ Moncrieff (2001) showed that convection in background easterly winds is organized in a two-scale
⁷⁶ structure with a synoptic-scale envelope moving eastward and numerous embedded MCSs moving
⁷⁷ westward. Slawinska et al. (2014) showed that the Walker circulation over a warm pool exhibits
⁷⁸ intraseasonal variability with outward (inward) moving synoptic-scale systems during its expan-
⁷⁹ sion (contraction) phases. Due to expensive computational cost, many three-dimensional (3-D)
⁸⁰ CRM simulations only focused on radiative convective equilibrium in small domains (Held et al.
⁸¹ 1993; Bretherton et al. 2005). In the absence of rotation, those disordered and scattered small-scale
⁸² clouds arising from initial disturbances in a moist unstable environment coalesce into large-scale
⁸³ patches of convection, which is known as self-aggregation (Bretherton et al. 2005; Muller and
⁸⁴ Held 2012; Wing and Emanuel 2014). Bretherton et al. (2005) recognized the self-aggregation
⁸⁵ as an instability driven by convection-water vapor-radiation-surface fluxes feedbacks. However,
⁸⁶ those theories for explaining large-scale organization of convection mostly focus on thermody-

87 namic effects, while dynamic effects due to multi-scale interactions are overlooked. Moreover, the
88 absence of rotation makes the model setup less realistic.

89 In fact, several studies have been conducted to investigate the effects of rotation on scale selec-
90 tion and multi-scale organization of convection. Majda et al. (2015) used the multicloud model
91 (Khouider and Majda 2006c,a,b, 2007) with either a deterministic (Khouider and Majda 2008b,a)
92 or stochastic (Khouider et al. 2010; Deng et al. 2015; Goswami et al. 2017) convective heating
93 closure to simulate organized convection in a rotating 2-D flow. They concluded that the planetary
94 rotation is one of important players in the diminishing of organized convection and convectively
95 coupled gravity wave activity, and deep convection activity in the stochastic model simulations
96 becomes patchy and unorganized in the subtropics and mid-latitudes. The 2-D nonhydrostatic
97 anelastic model simulation by Liu and Moncrieff (2004) indicated that rotation-induced localized
98 descent stabilizes and dries the neighborhood of convective region, explaining the fact that the
99 tropics is a preferred region for convective clustering. In general, planetary rotation has significant
100 impact on background sounding of thermodynamic fields and vertical shear, the latter of which
101 plays a crucial role in promoting organized convection (Newton and Rodebush Newton 1959;
102 Moncrieff 1981; Moncrieff and Liu 1999; Tompkins 2001).

103 The goals of this paper include the following four aspects, 1) using a global 2-D CRM to sim-
104 ulate multi-scale organization of convection in three regimes with weak, order-one, and strong
105 rotation, respectively; 2) deriving a multi-scale asymptotic model for upscale and downscale im-
106 pacts in each rotation regime and using it as a diagnostic framework for energy budget analysis; 3)
107 explaining why planetary-scale organization diminishes in the weak rotation regime as the magni-
108 tude of rotation increases and investigating the role of eddy transfer of momentum, temperature,
109 and equivalent potential temperature from meso- and synoptic-scale fluctuations; 4) explaining

¹¹⁰ why synoptic-scale organization persists in the order-one rotation regime but diminishes in the
¹¹¹ strong rotation regime.

¹¹² Here we use the System for Atmospheric Modeling (SAM) (Khairoutdinov and Randall 2003) to
¹¹³ investigate the effects of rotation on the multi-scale organization of convection. Thanks to its easy
¹¹⁴ configuration and fast execution, the SAM model has been used widely to simulate large-scale or-
¹¹⁵ ganization of convection in idealized domain geometry (Bretherton et al. 2005; Wing and Emanuel
¹¹⁶ 2014; Bretherton and Khairoutdinov 2015; Wing and Cronin 2016). In particular, Brenowitz et al.
¹¹⁷ (2018) configured the model in a global 2-D periodic domain to simulate organized convection
¹¹⁸ without the rotation. With both radiative cooling and surface fluxes fixed, the simulation in back-
¹¹⁹ ground easterly winds still produces an eastward-moving planetary-scale envelope of convection
¹²⁰ with multiple superclusters of cloudiness and numerous embedded clusters. To identify phys-
¹²¹ ical mechanisms behind the multi-scale organization, Brenowitz et al. (2018) decomposed the
¹²² model outputs into meso-, synoptic-, and planetary-scale components and concluded the key role
¹²³ of multi-scale interactions in promoting large-scale organization of convection based on energy
¹²⁴ budget analysis. Here we configure the SAM model in a similar way as Brenowitz et al. (2018)
¹²⁵ but with the Coriolis force. The magnitude of rotation is varied to represent three different regimes,
¹²⁶ including the ITCZ regime with weak rotation, the Indian monsoon trough regime with order-one
¹²⁷ rotation, and the mid-latitude regime with strong rotation.

¹²⁸ In each regime, we derive a multi-scale model by following the multi-scale asymptotic methods
¹²⁹ (Majda and Klein 2003; Majda 2007) and use it as a diagnostic framework for energy budget anal-
¹³⁰ ysis. In particular, the multi-scale models in the weak and order-one rotation regimes are derived
¹³¹ under the standard physical scaling in the tropics (Majda 2007). Consequently, the governing
¹³² equations across synoptic- and meso-scales are similar to the mesoscale equatorial synoptic dy-
¹³³ namics (MESD) model (Majda 2007), and those across planetary- and synoptic-scales resemble

134 the intraseasonal multi-scale moist dynamics (IMMD) model (Biello and Majda 2010; Back and
135 Biello 2018). Notably, the MESD model has been used to study the upscale impact of MCSs
136 on convectively coupled Kelvin waves (CCKWs) (Yang and Majda 2017, 2018) and 2-day waves
137 (Yang and Majda 2019). In contrast, the multi-scale model in the strong rotation regime follows
138 the classic quasi-geostrophic (QG) scaling (Vallis 2017).

139 We run 10 SAM model simulations under the similar configuration as Brenowitz et al. (2018) but
140 with increasing magnitude of rotation. Several key results about the effects of rotation are obtained.
141 First of all, planetary-scale organization of convection only arises in the weak rotation regime,
142 while synoptic-scale organization persists in the order-order rotation regime but diminishes as the
143 magnitude of rotation further increases. As summarized by the schematic diagram in Fig. 9,
144 the diminishment of planetary-scale organization is attributed to two changing effects in terms of
145 planetary kinetic energy budget of zonal winds, including decreasing acceleration effect by eddy
146 zonal momentum transfer from mesoscale fluctuations and increasing deceleration effect by the
147 Coriolis force. As for the acceleration effect from upscale impact of MCSs, its decreasing strength
148 is attributed to less favorable conditions for convection provided by background sounding of both
149 low-level equivalent potential temperature and vertical shear of zonal winds, resulting from the
150 increasing magnitude of rotation. Similarly, the maintenance of synoptic-scale organization in
151 the order-one rotation regime and its diminishment in strong rotation regime is also related to the
152 decreasing acceleration effect from upscale impact of MCSs, as summarized by the schematic
153 diagram in Fig.15.

154 The rest of the paper is organized as follows. Section 2 describes the model configuration and
155 experiment design. Section 3 shows the spatio-temporal variability of brightness temperature and
156 the zonal-mean climatology of winds and thermodynamic fields with different magnitude of ro-
157 tation. A multi-scale decomposition method is introduced to decompose total fields into domain-

158 mean and planetary-, synoptic-, meso-scale fluctuations. Section 4 investigates the planetary-scale
159 kinetic energy budget of zonal and meridional winds and available potential energy in the weak
160 rotation regime, and highlights the key role of eddy transfer of momentum, temperature, and equiv-
161 alent potential temperature. Section 5 does a similar energy budget analysis for synoptic-scale flow
162 fields in the order-one rotation regime, while Section 6 considers the strong rotation regime. The
163 paper concludes with a discussion in Section 7.

164 2. Model Configuration and Experiment Design

165 The SAM model version 6.11.1 is used here under the similar configuration as the QSTRAT
166 simulation in Brenowitz et al. (2018) but with the Coriolis force. All simulations use the single-
167 moment microphysics and the CAM3 radiation packages, Smolarkiewicz's MPDATA advection
168 scheme with monotonic corrector, and the 1.5-order closure (prognostic SGS turbulent kinetic
169 energy) subgrid-scale scheme. In order to exclude effects of surface fluxes, we perform all sim-
170 ulations over a uniform 300.15 K sea surface temperature (SST) ocean surface with latent and
171 sensible heat fluxes fixed at 210.6 W m^{-2} and 31.20 W m^{-2} , respectively. To avoid effects of ac-
172 tive radiation, we prescribe a fixed radiative cooling of 1.5 K day^{-1} below 150 hPa and a constant
173 stratospheric heating of 4.5 K day^{-1} above. The stratospheric heating increases stratification of
174 the atmosphere near the tropopause, turning the troposphere into a rigid-lid scenario. Similar to
175 Grabowski and Moncrieff (2001), the zonal winds are nudging towards -10 ms^{-1} easterly back-
176 ground winds with nudging time scale 1 day. A sponge layer is added at the domain top to damp
177 gravity waves. The 2-D planetary domain has $2^{15} = 32768$ km zonal extent in a 2 km horizontal
178 resolution and 27 km vertical extent with 64 vertical levels. All simulations are run for 100 days,
179 and the last 80-day solutions are used for diagnostic analysis.

180 Here we repeat the non-rotating simulation in Brenowitz et al. (2018) as the control experiment
181 and run another 9 simulations with increasing magnitude of rotation from the tropics to the mid-
182 latitude in the Northern Hemisphere (NH). The counterparts in the Southern Hemisphere can be
183 induced based on the mirror symmetry about the equator. It is worth mentioning that the standard
184 synoptic time scale is about 8 hrs (Majda 2007), equivalent to the reciprocal of Coriolis frequency
185 f at the latitude 14 deg N. As shown by Table 1, we divide all rotating scenarios into three regimes,
186 including i) the ITCZ regime with weak rotation ($0 \sim 6^\circ$ N), ii) the Indian monsoon trough regime
187 with order-one rotation ($6^\circ \sim 20^\circ$ N), and iii) the mid-latitude regime with strong rotation ($> 20^\circ$
188 N). We choose these three rotation regimes, not only because of the observation that convection
189 exhibits distinct characteristics in the tropics, subtropics, and mid-latitudes, but also the different
190 properties of governing equations as shown in Table 2-4. Besides, the second regime is referred to
191 as the order-one rotation regime, because the corresponding Coriolis frequency is comparable to
192 its standard value at the latitude 14 deg N.

193 **3. Effects of Rotation on the Multi-scale Organization of Convection**

194 In this section, we first study the spatio-temporal variability of brightness temperature and 850-
195 hPa zonal winds, which represent thermodynamic and dynamic aspects of convection, respectively.
196 Notably, Fig.1 and Fig.2 show that planetary-scale organization of convection only arises in the
197 weak rotation regime, while synoptic-scale organization persists in the order-one rotation regime
198 but diminishes in the strong rotation regime. The effects of rotation on zonal-mean climatology of
199 flow fields are also investigated.

200 a. Spatio-temporal variability of brightness temperature and 850-hPa zonal winds

201 Fig. 1a shows the Hovmöller diagram of brightness temperature in the non-rotating case, which
202 is the same as Brenowitz et al. (2018). In the first 5 days, numerous westward-moving MCSs
203 are organized into a few eastward-moving synoptic-scale envelopes. After that, a planetary-scale
204 envelope of convection at wavenumber 2 gradually forms and propagates eastward at a speed of 7
205 m/s. This planetary-scale envelope contains several eastward-moving synoptic-scale disturbances
206 in the leading edge and westward-moving disturbances in the trailing edge with numerous embed-
207 ded westward-moving MCSs. Fig. 1b-h are for the remaining 7 cases (last 2 cases in the strong
208 rotation regime are not shown). In the weak rotation regime, the planetary-scale organization of
209 convection arises at the latitude 1° N in panel (b) but diminishes in panels (c) and (d). In con-
210 trast, panels (e-g) show that synoptic-scale envelopes with embedded westward-moving MCSs
211 dominate in the order-one rotation regime, resembling the two-scale organization of convection
212 in Grabowski and Moncrieff (2001). As the magnitude of rotation increases, the length scale of
213 synoptic-scale envelopes becomes smaller, while their propagation speed is faster. At the latitude
214 27° N in panel (h) in the strong rotation regime, scattered MCSs prevail over the whole domain,
215 which is akin to the mid-latitude case in Liu and Moncrieff (2004).

216 Fig. 2a shows the wavenumber-frequency spectra of brightness temperature in the non-rotating
217 case. The spectra of brightness temperature is dominated by a peak at wavenumber 2 and period
218 of 26.7 days, which further extends to larger wavenumber and shorter period along a straight line
219 across the origin. In contrast, the spectra of westward-moving modes is much weaker. Fig. 2b
220 shows the spectra of 850-hPa zonal velocity, which is similar to panel (a) but with the significant
221 spectra of westward-moving modes at wavenumber 1-5. Fig. 2c-r are for the remaining 8 cases
222 (last case in the strong rotation regime is not shown). Panels (c) and (d) at the latitude 1° N

223 resemble panels (a) and (b). As the magnitude of rotation increases in the weak rotation regime, the
224 spectra accounting for eastward-moving envelopes gradually shifts to smaller spatial and temporal
225 scales in panels (e-j). It is worth mentioning that the period of eastward-moving envelopes are
226 longer than the corresponding time scale of the Coriolis force. Panels (k-r) show the spectra in the
227 order-one and strong rotation regimes. Overall, the maximum strength of spectra decays gradually
228 as the magnitude of rotation increases, indicating the diminishing spatio-temporal variability of
229 convection. Besides, the spectra band of westward-moving modes shifts along with the peak of
230 eastward-moving envelopes, reflecting the modulation effect by the latter.

231 *b. Zonal-mean climatology of winds, moisture, and (equivalent) potential temperature*

232 Fig. 3 shows the zonal-mean climatology of zonal and meridional velocity, density, water vapor,
233 and (equivalent) potential temperature. As shown by panel (a), zonal winds in the non-rotating
234 case feature significant anomalies from -10 ms^{-1} background easterly winds throughout the tro-
235 posphere, including weak winds below 950 hPa due to boundary layer (BL) friction and easterly
236 (westerly) anomalies in the lower (upper) troposphere. The vertical shear in the free troposphere
237 diminishes gradually as the magnitude of rotation increases, while that in the BL keeps unchanged.
238 In contrast, the presence of the Coriolis force induces significant meridional winds in panel (b)
239 with northerlies below 950 hPa, southerlies between 950 hPa and 600 hPa, and northerlies above
240 400 hPa. Vertical profiles of density, potential temperature are mostly similar among all cases in
241 panels (c) and (d). As shown by panel (e), water vapor decreases exponentially in height with
242 most of water vapor contained below 600 hPa. Equivalent potential temperature in panel (f) is
243 characterized by negative vertical gradient below 700 hPa and positive vertical gradient above that
244 level. As the magnitude of rotation increases, the lower and middle troposphere become more
245 moist near 700 hPa with larger value of moisture and equivalent potential temperature. The result-

246 ing reduced vertical gradient of equivalent potential temperature in the lower troposphere provides
247 less favorable conditions for convection.

248 *c. Multi-scale decomposition of flow fields across planetary-, synoptic- and meso-scales*

249 In order to facilitate diagnostic analysis for multi-scale interactions in the following sections, we
250 introduce a multi-scale decomposition method based on the coarse-graining technique, a straight-
251 forward generalization of asymptotic averaging operators (Majda 2007) in a finite domain with
252 small grid spacing. The detailed procedure for decomposing total fields into domain mean, and
253 planetary-, synoptic-, meso-scale fluctuations is explained below. Suppose f is the total field and
254 f_{res} is the residual. Initially, let $f_{res} = f$.

255 **Step 1:** calculate the mean value of f_{res} in the whole domain and denote it as \bar{f} for domain-
256 mean.

257 **Step 2:** update the residual, $f_{res} = f - \bar{f}$, calculate the mean value of f_{res} over a coarse grid with
258 2000 km spacing, and denote it as f^p for planetary-scale fluctuations.

259 **Step 3:** update the residual, $f_{res} = f - \bar{f} - f^p$, calculate the mean value of f_{res} over a coarse grid
260 with 256 km spacing, and denote it as f^* for synoptic-scale fluctuations.

261 **Step 4:** update the residual, $f_{res} = f - \bar{f} - f^p - f^*$, calculate the mean value of f_{res} over a coarse
262 grid with 16 km spacing, and denote it as f' for mesoscale fluctuations.

263 The coarse grid spacing (2000 km, 256 km, 16 km) is chosen so that 10 coarse grids (20000
264 km, 2560 km, 160 km) are able to resolve planetary-, synoptic- and meso-scale fluctuations, re-
265 spectively. In practice, we first coarse grain the total fields onto coarse grids of 16 km to save
266 computing expense and filter out fluctuations on smaller scales below 16 km. Such a residual
267 based technique for multi-scale decomposition is similar to that in Brenowitz et al. (2018), except
268 that the latter uses the low-pass filter in the Fourier domain. Fig.4 gives an example for decom-

269 posing brightness temperature from the non-rotating case by using this multi-scale decomposition
270 method. This method successfully captures the spatio-temporal variability of convection across
271 multiple scales, including eastward-moving planetary-scale envelopes in panel (b), synoptic-scale
272 eastward- and westward-moving disturbances in panel (d) and prevalent westward-moving MCSs
273 in panel (e). The domain mean field in panel (c) is steady with negligible variance.

274 4. The ITCZ Regime with Weak Rotation

275 In this section, we focus on the ITCZ regime with weak rotation ($0 \sim 6^\circ$ N). Typical regions
276 in this regime include the warm pool region from the Indian Ocean to the West Pacific and the
277 ITCZ region over the East Pacific (Waliser and Gautier 1993; Yang et al. 2017). Here we first
278 derive a multi-scale model with weak rotation across the planetary-, synoptic- and meso-scales
279 by following the systematic multi-scale asymptotic theory (Majda and Klein 2003; Majda 2007).
280 Then we use it as a diagnostic framework for energy budget analysis to understand why planetary-
281 scale organization of convection diminishes in this regime, as shown by Fig. 1a-d.

282 *a. A multi-scale model with weak rotation for interactions of convection across planetary-,
283 synoptic- and meso-scales*

284 In general, multi-scale asymptotic models are useful for capturing leading-order scale interac-
285 tions of convection across multiple spatial and temporal scales (Yang and Majda 2014; Majda
286 and Yang 2016; Yang et al. 2017). The derivation of this multi-scale model starts from the 2-D
287 anelastic primitive equations on the f plane. The Froude number $\varepsilon = 0.1$ is chosen as the small
288 parameter for multi-scale asymptotic analysis. According to the standard scaling (Majda 2007),
289 synoptic-scale spatial and temporal coordinates (x, t) have dimensional units of $(1500\text{km}, 8.3\text{hrs})$.
290 Correspondingly, the planetary-scale spatial and temporal coordinates (X, T) have dimensional

291 units ($15000\text{km}, 3\text{days}$) that are $\frac{1}{\varepsilon} = 10$ times of synoptic scales, while meso-scale coordinates
 292 (x', τ) are $\varepsilon = \frac{1}{10}$ of synoptic scales. As for physical variables, zonal and meridional velocity,
 293 (u, v) , are scaled in a unit of 50 ms^{-1} , and vertical velocity w in a unit of 0.16 ms^{-1} . Pressure
 294 perturbation p is scaled in a unit of $2500 \text{ m}^2\text{s}^{-2}$, potential temperature anomalies θ and mois-
 295 ture anomalies q in a unit of 15 K , and diabatic heating s_θ in a unit of 45 K day^{-1} . The order of
 296 variables are summarized in the third column of Table 2. In order to separate terms into different
 297 scales, spatial averaging operator \bar{u} and temporal averaging operator $\langle u \rangle$ for an arbitrary variable
 298 u , and the superscripts p, s indicates the averaging on planetary and synoptic scales, respectively.

299 This multi-scale model consists of four groups of equations, each of which governs dynamics on
 300 one specific spatial temporal scales. In detail, the first group of equations at the 3rd row of Table 2
 301 describe trade wind dynamics on the planetary/intraseasonal scale as a climatological background.
 302 In contrast, the second group of equations at the 4th row describes the planetary/intraseasonal
 303 anomalies under the effects of rotation, which are also influenced by the advection of background
 304 flow U, W and interaction terms involving trade wind fields, U, Θ, Q . Furthermore, the eddy trans-
 305 fer of zonal momentum from synoptic fluctuations, $-\rho_0^{-1} (\rho_0 \langle \bar{w}^* \bar{u}^* \rangle^p)_z$ and that from mesoscale
 306 fluctuations, $-\rho_0^{-1} (\rho_0 \langle \bar{w}' \bar{u}' \rangle^p)_z$ represent upscale impact of synoptic- and meso-scale dynamics.
 307 Similar eddy terms also appear at the right hand side of meridional momentum, potential temper-
 308 ature, and moisture equations. The third group of equations at the 5th row govern the dynamics
 309 of synoptic-scale fluctuations, which is affected by the trade wind fields as well as eddy terms
 310 from mesoscale fluctuations. The last group of equations at the 6th row describe the dynamics of
 311 mesoscale fluctuations advected by trade wind fields.

312 b. Effects of eddy momentum transfer on planetary-scale momentum and kinetic energy budget

313 According to the governing equations for planetary-scale zonal and meridional momentum in
 314 Table 2,

$$\frac{Du}{Dt} + uU_X + wU_z - \hat{f}V = -px - \hat{d}u - \rho_0^{-1} (\rho_0 \langle \overline{w^*u^*} \rangle^p)_z - \rho_0^{-1} (\rho_0 \langle \overline{w'u'} \rangle^p)_z, \quad (1)$$

$$\frac{DV}{Dt} + \hat{f}u = -\hat{d}V - \rho_0^{-1} (\rho_0 \langle \overline{w^*v^*} \rangle^p)_z - \rho_0^{-1} (\rho_0 \langle \overline{w'v'} \rangle^p)_z, \quad (2)$$

315 where the trade wind background U is assumed to be -10 ms^{-1} . After taking the climatological-
 316 mean $[\cdot]$ (zonal and time averaging), the above equations are rewritten as,

$$[u_T] = [\hat{f}V] + [-\hat{d}u] + \left[-\rho_0^{-1} (\rho_0 \langle \overline{w^*u^*} \rangle^p)_z \right] + \left[-\rho_0^{-1} (\rho_0 \langle \overline{w'u'} \rangle^p)_z \right], \quad (3)$$

$$[V_T] = [-\hat{f}u] + [-\hat{d}V] + \left[-\rho_0^{-1} (\rho_0 \langle \overline{w^*v^*} \rangle^p)_z \right] + \left[-\rho_0^{-1} (\rho_0 \langle \overline{w'v'} \rangle^p)_z \right], \quad (4)$$

317 which indicate that eddy momentum transfer from synoptic- and meso-scale fluctuations influ-
 318 ences the planetary-scale winds.

319 Fig. 5a-c show the climatological-mean vertical profiles of eddy zonal momentum transfer from
 320 meso-, synoptic- and planetary-scale fluctuations. In detail, the eddy momentum transfer from
 321 mesoscale fluctuations in panel (a) induces westward (eastward) momentum forcing in the lower
 322 (middle and upper) tropospheres. Its magnitude gets weakened in both the upper and lower tro-
 323 pospheres as the latitude increases. In contrast, eddy momentum transfer from synoptic-scale
 324 fluctuations in panel (b) is negligible, while that from planetary-scale fluctuations in panel (c) has
 325 significant momentum forcing only above 600 hPa. In addition, panel (d) and (e) show the Coriolis
 326 force term and momentum drag, both of which have the opposite vertical profiles as that in panel
 327 (a). As the latitude increases, the momentum damping effect in panel (d) gets strengthened, while
 328 that in panel (e) gets weakened.

Fig. 6(a-c) shows the climatological-mean vertical profiles of eddy meridional momentum transfer from meso-, synoptic- and planetary-scale fluctuations. In detail, the eddy meridional momentum transfer from mesoscale fluctuations induces both low-level and middle-tropospheric southward momentum forcing and upper-tropospheric northward momentum forcing, while that from synoptic fluctuations is negligible. The eddy momentum transfer from planetary-scale fluctuations induces northward momentum forcing in the upper troposphere and southward momentum force near the tropopause. The Coriolis force and momentum damping in panels (d) and (e) have the similar vertical profiles but in the opposite signs.

After multiplying Eqs. 1 and 2 by $\rho_0 u$ and $\rho_0 v$ respectively and taking climatological mean, we can obtain the planetary kinetic energy budget equations,

$$\left[\left(\frac{1}{2} \rho_0 u^2 \right)_T \right] = [\rho_0 \hat{f} V u] + [-\rho_0 p_x u] + [-\hat{d} \rho_0 u^2] + \left[-(\rho_0 \langle \overline{w^* u^*} \rangle^p)_z u \right] + \left[-(\rho_0 \langle \overline{w' u'} \rangle^p)_z u \right], \quad (5)$$

$$\left[\left(\frac{1}{2} \rho_0 V^2 \right)_T \right] = [-\rho_0 \hat{f} u V] + [-\hat{d} \rho_0 V^2] + \left[-(\rho_0 \langle \overline{w^* v^*} \rangle^p)_z V \right] + \left[-(\rho_0 \langle \overline{w' v'} \rangle^p)_z V \right]. \quad (6)$$

Fig.7a-c show the vertical profiles of energy source and sink terms in the planetary-scale kinetic energy budget for zonal winds. Panel (a) shows the deceleration term involving the Coriolis force, which transfers kinetic energy from zonal winds to meridional winds. In contrast, both terms involving synoptic- and meso-scale fluctuations in panels (b) and (c) induce acceleration effects in both lower and upper tropospheres, whose magnitudes decrease gradually as the latitude increases. Fig. 7d-f are for meridional winds. As shown by panel (e), the term involving eddy momentum transfer from synoptic-scale fluctuations is negligible at levels below 400 hPa but induces acceleration/deceleration effects above that level. In contrast, the term involving eddy meridional momentum transfer from mesoscale fluctuations in panel (f) always induces deceleration effects throughout the troposphere.

Fig. 8a-b show the planetary-scale kinetic energy budget for zonal and meridional winds. The first term for time tendency has negligible value in both panels. As shown by panel (a), eddy momentum transfer from both synoptic- and meso-scale fluctuations induce acceleration effect, while the terms involving the Coriolis force, pressure gradient and momentum damping induce deceleration effect. As the latitude increases from 0 deg to 1,3,5 deg, acceleration effect induced by both eddy momentum transfer term gets weakened, while the Coriolis force term increases dramatically. Besides, both the terms involving pressure gradient and damping decrease as the latitude increases. As shown by panel (b), the term involving eddy meridional momentum transfer from synoptic-scale fluctuations induces weak acceleration effect, while that from mesoscale fluctuations and the damping term induce significant deceleration effect.

Fig. 9a shows the schematic diagram for planetary-scale kinetic energy budget in the weak rotation regime. According to Fig.8a, the dominant acceleration effect comes from the term involving eddy zonal momentum transfer from mesoscale fluctuations $[-(\rho_0 \langle w'u' \rangle^P)_z u]$, while the dominant deceleration effect comes from the term involving the Coriolis force $[\rho_0 \hat{f} Vu]$. As the magnitude of rotation increases, this acceleration effect decreases dramatically while the deceleration effect increases instead. The resulting reduced planetary-scale kinetic energy budget of zonal winds explains the diminishing planetary-scale organized convection.

Both changed acceleration/deceleration effects should be traced back to the increasing magnitude of rotation, as it is the only difference in the model input. In fact, the increasing deceleration term $[\rho_0 \hat{f} Vu]$ can be simply explained by the larger value of f at higher latitudes. As for the acceleration term $[-(\rho_0 \langle w'u' \rangle^P)_z u]$, its decreasing strength is attributed to less favorable conditions for MCSs provided by background sounding of both low-level equivalent potential temperature and low-level vertical shear of zonal winds as shown in Fig. 9b. According to Fig. 3f, the low-level equivalent potential temperature between 600-800 hPa increases by a few Kelvin as the

magnitude of rotation increases, leading to larger convective inhibition (CIN) and less moist instability. Meanwhile, the Coriolis term fV in Fig. 5d induces a momentum forcing in the opposite sign as the climatological mean zonal winds in Fig. 3a, resulting in reduced low-level vertical shear.

c. Effects of eddy heat transfer on planetary-scale heat and available potential energy budget

The governing equation for planetary-scale potential temperature anomalies in Table 2 reads as follows,

$$\theta_T + U\theta_X + N^2w = -\hat{d}_\theta\theta - \rho_0^{-1} \left(\rho_0 \langle \overline{w^*\theta^*} \rangle^P \right)_z - \rho_0^{-1} \left(\rho_0 \langle \overline{w'\theta'} \rangle^P \right)_z + s_\theta, \quad (7)$$

where the trade wind background is assumed to be $U = -10ms^{-1}$ and $\Theta = 0K$. The corresponding climatological-mean equation is,

$$[\theta_T] = [-N^2w] + [-\hat{d}_\theta\theta] + \left[-\rho_0^{-1} \left(\rho_0 \langle \overline{w^*\theta^*} \rangle^P \right)_z \right] + \left[-\rho_0^{-1} \left(\rho_0 \langle \overline{w'\theta'} \rangle^P \right)_z \right] + [s_\theta]. \quad (8)$$

Fig.10 show the climatological-mean vertical profiles of eddy heat transfer from meso-, synoptic- and planetary-scale fluctuations. Unlike Fig. 5 and 6, the vertical profiles of all eddy terms do not change much as the latitude increases, indicating that these terms are not directly responsible for the diminishment of planetary-scale organization of convection. In fact, both eddy heat transfer from synoptic- and meso-scale fluctuations introduces heating in the lower troposphere and increases CIN, providing unfavorable conditions for convection. In contrast, the eddy heat transfer from planetary-scale fluctuations in panel (c) only induces heating/cooling effects above 500 hPa.

390 After multiplying Eq.7 by $\frac{\rho_0 \theta}{N^2}$ and taking climatological mean, the governing equation for avail-
 391 able potential energy budget is obtained below,

$$\left[\left(\rho_0 \frac{\theta^2}{2N^2} \right)_T \right] = [-\rho_0 w \theta] + \left[-\rho_0 \hat{d}_\theta \frac{\theta^2}{N^2} \right] + \left[-\left(\rho_0 \langle \overline{w^* \theta^*} \rangle^p \right)_z \frac{\theta}{N^2} \right] + \left[-\left(\rho_0 \langle \overline{w' \theta'} \rangle^p \right)_z \frac{\theta}{N^2} \right] + \left[\rho_0 s_\theta \frac{\theta}{N^2} \right], \quad (9)$$

392 where the term $[-\rho_0 w \theta]$ transfers energy between kinetic energy and available potential energy.

393 Fig.11 shows the climatological-mean vertical profiles of energy source and sink terms in avail-
 394 able potential energy budget. The energy transfer term in panel (a) is characterized by the second
 395 baroclinic mode with upper-tropospheric (lower-tropospheric) energy sink (source) in a decreas-
 396 ing magnitude. As shown by panels (b) and (c), the energy source/sink terms involving eddy
 397 heat transfer from synoptic- and meso-scale fluctuations share the similar vertical profiles, both of
 398 which feature an energy source below 850 hPa and above 300 hPa, and an energy sink between
 399 350-850 hPa. Meanwhile, neither term changes much throughout the troposphere as the latitude
 400 increases, indicating that these terms are not directly responsible for the diminishing planetary-
 401 scale organization.

402 *d. Effects of eddy transfer of equivalent potential temperature on the planetary-scale atmospheric
 403 stability*

404 Similar to Eq.8, the governing equation for equivalent potential temperature, θ_e , reads as follows,

$$[(\theta_e)_T] = [-N_e^2 w] + [-\hat{d}_\theta \theta_e] + \left[-\rho_0^{-1} \left(\rho_0 \langle \overline{w^* \theta_e^*} \rangle^p \right)_z \right] + \left[-\rho_0^{-1} \left(\rho_0 \langle \overline{w' \theta'_e} \rangle^p \right)_z \right], \quad (10)$$

405 where N_e represents background stratification of equivalent potential temperature.

406 Fig.12 shows the climatological-mean vertical profiles of eddy transfer of equivalent potential
 407 temperature from planetary-, synoptic- and meso-scale fluctuations. Among these three terms,
 408 eddy terms from synoptic- and meso-scale fluctuations dominate and induce cooling and drying

409 effects below 850 hPa and heating and moistening effects above that level. The eddy term from
410 planetary fluctuations have negligible magnitude throughout the troposphere. As shown by panel
411 (d), the total eddy heat transfer features significant positive vertical gradient in the lower tropo-
412 sphere, which tends to reduce the atmospheric instability and provide unfavorable conditions for
413 convection. It is worth mentioning that these vertical profiles do not change as the magnitude of
414 rotation increases.

415 **5. The Indian Monsoon Regime with Order-One Rotation**

416 In this section, we will focus on the Indian Monsoon regime with order-one rotation ($6^\circ \sim 20^\circ N$).
417 A typical region in this regime is the monsoon trough over the Indian subcontinent (Gadgil 2003).
418 As shown by Fig.1e-g, large-scale convection is dominated by synoptic-scale envelopes that move
419 eastward at a speed of 15 m/s, resembling the simulation by Grabowski and Moncrieff (2001). It is
420 important to investigate the upscale impact of MCSs on synoptic-scale dynamics and understand
421 why synoptic-scale organization persists in this regime.

422 Table 3 shows the multi-scale model for the scale interactions across meso-, synoptic- and
423 planetary-scales in the order-one rotation regime. To derive this multi-scale model, we use the
424 same physical scaling for all physical variables as Section 4a, except for the Coriolis force pa-
425 rameter f in the order-one magnitude. Thus, the two models in Table 2 and 3 share many similar
426 features. The major difference lies in the fact that trade wind background and synoptic-scale dy-
427 namics in Table 3 feel the Coriolis force. Moreover, this three-scale model can be regarded as the
428 coupling between the IMMD model (Biello and Majda 2010) for planetary- and synoptic-scale
429 interactions and the MESD model (Majda 2007) for synoptic- and meso-scale interactions.

431 According to Table 3, synoptic-scale dynamics is driven by eddy transfer of momentum, tem-
 432 perature and moisture from mesoscale fluctuations. It should be interesting to investigate the up-
 433 scale impact of MCSs on synoptic-scale organization of convection in this regime. The governing
 434 equations for synoptic-scale kinetic energy budget of zonal and meridional winds and available
 435 potential energy budget read below,

$$\left[\left(\frac{1}{2} \rho_0 (u^*)^2 \right)_t \right] = [\rho_0 \hat{f} v^* u^*] + [-\rho_0 p_x^* u^*] + \left[- \left(\rho_0 \langle w' u' \rangle^s \right)_z u^* \right], \quad (11)$$

$$\left[\left(\frac{1}{2} \rho_0 (v^*)^2 \right)_t \right] = [-\rho_0 \hat{f} v^* u^*] + \left[- \left(\rho_0 \langle w' v' \rangle^s \right)_z v^* \right], \quad (12)$$

$$\left[\left(\rho_0 \frac{(\theta^*)^2}{2N^2} \right)_t \right] = [-\rho_0 w^* \theta^*] + \left[- \left(\rho_0 \langle w' \theta' \rangle^s \right)_z \frac{\theta^*}{N^2} \right] + \left[\rho_0 s_\theta^* \frac{\theta^*}{N^2} \right]. \quad (13)$$

436 Fig.13 shows the climatological-mean vertical profiles of energy source/sink terms on the
 437 synoptic-scale kinetic and available potential energy budgets. It turns out that eddy zonal mo-
 438 mentum transfer in panel (a) induces acceleration effects throughout the troposphere, whose mag-
 439 nitude decays gradually as the latitude increases. In contrast, eddy meridional momentum transfer
 440 in panel (b) induces weaker deceleration effects, while eddy heat transfer in panel (c) induces
 441 alternate energy source and sink at different levels. Besides, the Coriolis force term in panel (d)
 442 transfers kinetic energy from zonal winds to meridional winds, leading to deceleration effect in the
 443 kinetic energy budget of zonal winds. The term involving pressure gradient in panel (e) induces
 444 acceleration (deceleration) effect below (above) 850 hPa. In addition, the energy transfer term be-
 445 tween kinetic and available potential energy in panel (f) is characterized by the second baroclinic
 446 mode with low-level (upper-level) energy source (sink).

447 Fig.14 shows the synoptic-scale kinetic energy budget for zonal and meridional winds. The time
 448 tendency term in both panels (a) and (b) has negligible value. The acceleration/deceleration effects

449 induced by the Coriolis force do not change much. As for kinetic energy of zonal winds in panel
 450 (a), the dominant acceleration effect due to eddy zonal momentum transfer from mesoscale fluc-
 451 tuations decays as the latitude increases. Correspondingly, the deceleration effect due to pressure
 452 gradient also decays. As for meridional winds, the acceleration effect induced by the Coriolis force
 453 is balanced by the term involving eddy meridional momentum transfer and the damping residual.
 454 The residual in panel (b) is too large to be ignored and behaves as momentum dissipation, presum-
 455 ably due to the frictional effect from unorganized convection below the mesoscale that has been
 456 excluded in the budget analysis.

457 Fig.15 shows the schematic diagram for synoptic-scale kinetic energy budget. According to Fig.
 458 14a, the dominant acceleration effect in synoptic kinetic energy of zonal winds is induced by eddy
 459 zonal momentum transfer from mesoscale fluctuations $\left[-\left(\rho_0 \langle w' u' \rangle^s \right)_z u^* \right]$, while the decelera-
 460 tion effect comes from the term involving the Coriolis force $[\rho_0 \hat{f} v^* u^*]$. Thus, this acceleration
 461 effect maintains the synoptic-scale organization of convection. As the latitude further increases,
 462 this acceleration effect decays gradually, while the deceleration effect is unchanged. The resulting
 463 reduced synoptic-scale kinetic energy of zonal winds explains the diminishment of synoptic-scale
 464 organization in the order-one and strong rotation regimes in Fig. 1e-h. Similar to the weak rotation
 465 regime, the decaying upscale impact of MCSs is attributed to less favorable conditions for convec-
 466 tion provided by background sounding of warmer low-level equivalent potential temperature and
 467 weaker low-level vertical shear of zonal winds at higher latitudes, as shown in Fig. 3.

468 **6. The Mid-Latitude Regime with Strong Rotation**

469 In this section, we consider the mid-latitude regime with strong rotation. As shown by Fig.1h,
 470 the solution in this regime is characterized by scattered and random MCSs prevailing in the whole

⁴⁷¹ domain. It is interesting to investigate the upscale impact of MCSs and understand the vanishment
⁴⁷² of synoptic-scale organization of convection in the strong rotation regime.

⁴⁷³ *a. A multi-scale model with strong rotation for interactions of convection across planetary-,
⁴⁷⁴ synoptic- and meso-scales*

⁴⁷⁵ It is well known that large-scale circulation at mid-latitudes is governed by the QG dynamics.
⁴⁷⁶ Thus the standard QG scaling (Vallis 2017) is adopted here. In details, synoptic-scale spatial
⁴⁷⁷ and temporal coordinates (x, t) have dimensional units of $(1000\text{km}, 28\text{hrs})$. Correspondingly, the
⁴⁷⁸ planetary-scale spatial coordinate X has dimensional units 10000km that are $\frac{1}{\varepsilon} = 10$ times of those
⁴⁷⁹ on the synoptic scale, while meso-scale coordinates (x', τ) are $\varepsilon = \frac{1}{10}$ of synoptic-scale ones. As
⁴⁸⁰ for physical variables, zonal and meridional velocity, (u, v) , are scaled in a unit of 10 ms^{-1} , and
⁴⁸¹ vertical velocity w in a unit of 0.1 ms^{-1} . Pressure perturbation p is scaled in a unit of $1000 \text{ m}^2\text{s}^{-2}$,
⁴⁸² potential temperature anomalies θ and moisture anomalies q in a unit of 3 K , and diabatic heating
⁴⁸³ s_θ in a unit of 2.57 Kday^{-1} .

⁴⁸⁴ Table 4 shows the multi-scale model in this strong rotation regime with three groups of equa-
⁴⁸⁵ tions, each of which governs one single scale dynamics. In brief, the planetary-scale dynamics
⁴⁸⁶ is governed by long-wave approximation equations, the synoptic-scale dynamics is governed by
⁴⁸⁷ QG equations, and the mesoscale dynamics is governed by the linear mesoscale equatorial weak
⁴⁸⁸ temperature gradient (MEWTG) equations (Majda and Klein 2003; Majda et al. 2008). Notably,
⁴⁸⁹ this multi-scale model is distinguished from the other two models in Table 2 and 3 by the absence
⁴⁹⁰ of eddy terms across planetary-, synoptic- and meso-scales. This multi-scale model predicts the-
⁴⁹¹oretically that upscale impact of synoptic- and meso-scale fluctuations is negligible in the strong
⁴⁹² rotation regime.

493 b. *Upscale impact of meso-scale fluctuations on synoptic-scale dynamics*

494 Fig. 16 shows the synoptic-scale kinetic energy budget for zonal and meridional winds in the
495 strong rotation regime. The overall features of all energy source and sink terms are similar to
496 those in Fig.14. In particular, eddy zonal momentum transfer from meso-scale fluctuations still
497 induces acceleration effect in the kinetic energy budgets, whose magnitude further decreases as the
498 latitude increases. In contrast, eddy meridional momentum transfer induces deceleration effects.
499 However, when compared with Fig.14, these acceleration/deceleration effects are too weak to
500 support synoptic-scale organization of convection. Unlike Fig.14, the deceleration effect due to
501 the Coriolis force gradually decreases as the rotation increases.

502 **7. Concluding Discussion**

503 This study is aimed at investigating the effects of rotation on the multi-scale organization of
504 convection with the following goals. First, we use a global 2-D CRM to simulate multi-scale
505 organization of convection in three rotation regimes (weak, order-one, and strong), representing
506 idealized ITCZ region ($0^\circ \sim 6^\circ$ N), Indian monsoon region ($6^\circ \sim 20^\circ$ N), and mid-latitude region
507 ($20^\circ \sim 45^\circ$ N), respectively. Secondly, we derive a multi-scale asymptotic model for upscale
508 and downscale impacts in each rotation regime and use it as a diagnostic framework for energy
509 budget analysis. Thirdly, we explain why planetary-scale organization diminishes in the weak
510 rotation regime as the magnitude of rotation increases and investigate the role of eddy transfer
511 of momentum, temperature, and equivalent potential temperature from meso- and synoptic-scale
512 fluctuations. Lastly, we explain why synoptic-scale organization persists in the order-one rotation
513 regime but diminishes in the strong rotation regime.

514 Here we use the 2-D version of the SAM model to simulate multi-scale organization of con-
515 vection with different magnitudes of rotation. In the weak rotation regime, planetary-scale orga-

516 nization of convection arises at the latitude 0 deg and 1° N, but diminishes as the magnitude of
517 rotation increases. The eastward-moving planetary-scale envelope contains several eastward- and
518 westward-moving synoptic-scale disturbances with numerous embedded MCSs. In the order-one
519 rotation regime, convection is organized in a two-scale structure with eastward-moving synoptic-
520 scale envelopes and westward-moving embedded MCSs. In the strong rotation regime, numerous
521 scattered and unorganized MCSs prevail in the whole domain. The effect of rotation on large-
522 scale organization of convection as revealed by this CRM simulation is consistent to that in Majda
523 et al. (2015). With both radiative cooling and surface fluxes fixed, the planetary-scale organization
524 of convection in our simulations is mainly due to the multi-scale interactions of flow fields, dis-
525 tinguishing itself from several previous theories that focus on convection-radiation-surface fluxes
526 feedbacks. (Bretherton et al. 2005; Wing and Emanuel 2014; Bretherton and Kharoutdinov 2015).

527 Here we divide all scenarios into three regimes (weak, order-one, and strong) in terms of the
528 magnitude of rotation. In each rotation regime, a three-scale model is derived by using the multi-
529 scale asymptotic method and used as a diagnostic framework to study the scale interactions of
530 convection across planetary-, synoptic- and meso-scales. Although they are reduced models from
531 the primitive equations, these multi-scale models presumably capture the leading-order quantities
532 of all flow fields with only small errors. The advantages of using these multi-scale models as a
533 diagnostic framework for budget analysis lie in three aspects, including i) modeling the scale inter-
534 actions of flow fields across multiple scales, ii) highlighting possible dominant terms in the energy
535 budget, iii) simplifying the diagnostic studies by ignoring secondary terms. By diagnostically cal-
536 culating energy budget based on these multi-scale models, we figure out energy transfer routes
537 on both planetary and synoptic scales and summarize them in the schematic diagrams in Fig. 9a
538 and Fig. 15. As shown by Fig. 9a, planetary kinetic energy of zonal winds is fueled by domi-
539 nant acceleration effect from MCSs and also that from synoptic convectively coupled waves, but

540 consumed through energy transfer to kinetic energy of meridional winds and available potential
541 energy as well as dissipation. The energy transfer routes on synoptic scale in Fig. 15 are similar
542 to those on planetary scale, reflecting the self-similarity property of convection (Majda 2007).

543 The results here highlight the crucial upscale impact of eddy zonal momentum transfer from
544 mesoscale fluctuations on both planetary- and synoptic-scale organization of convection. As the
545 magnitude of rotation increases, its acceleration effect on the planetary kinetic energy of zonal
546 winds decreases gradually, diminishing the planetary-scale organization of convection. Similarly,
547 due to its decreasing acceleration effect on synoptic kinetic energy of zonal winds, synoptic-scale
548 organization of convection only persists in the order-one rotation regime but diminishes in the
549 strong rotation regime. This indicates a need to parameterize upscale impact of MCSs in the
550 coarse-resolution GCMs. In fact, the MESD model (Majda 2007) theoretically predicts the sig-
551 nificant upscale impact of MCSs on eastward-moving CCKWs (Yang and Majda 2017, 2018) and
552 2-day waves (Yang and Majda 2019). Based on the explicit expressions of eddy terms obtained
553 from the MESD model, Yang et al. (2019) proposed a basic parameterization of upscale impact of
554 upshear-moving MCSs and showed that this parameterization significantly improves key features
555 of the MJO analog in a multicloud model. Moncrieff et al. (2017) introduced a parameteriza-
556 tion for collective effects of mesoscale organized convection that are missing in the contemporary
557 cumulus parameterization in the GCM.

558 The diminishing acceleration effects from MCSs are traced back to the increasing magnitude of
559 rotation, since it is the only difference in the model input among all simulations. As the magnitude
560 of rotation increases, both vertical gradient of equivalent potential temperature and vertical shear of
561 zonal winds in the lower troposphere decays, providing less favorable conditions for the generation
562 and propagation of MCSs. Consequently, their upscale impact on the planetary and synoptic
563 kinetic energy diminishes. The schematic diagram in Fig. 9b specifically depicts the effects of

564 increasing rotation on background sounding with less favorable conditions for promoting MCSs.
565 Such upscale and downscale impacts illustrate the crucial role of multi-scale interactions in scale
566 selection and organization of convection. Studying the effects of rotation should help improve
567 our fundamental understanding of large-scale organization of convection at different latitudes.
568 Besides, the MCSs in this 2-D CRM with rotation share several realistic features with 3-D CRMs,
569 while those in 2-D CRMs without rotation typically have an unrealistic strong circulation in the
570 zonal direction.

571 This study can be elaborated and extended in various ways. The implication of multi-scale
572 organization of convection presented here is limited due to the 2-D model configuration. Thus
573 one research direction is to implement the 3-D simulations and investigate the effects of rotation.
574 Meanwhile, the validity of using multi-scale asymptotic models as a diagnostic framework de-
575 pends on appropriate physical scaling for all flow fields and a good multi-scale decomposition
576 method for capturing the scale separation property of solutions. Another research direction is to
577 consider the multi-scale interactions of convection over the warm pool scenario. Also, it should
578 be interesting to consider the scenario in the presence of active radiation and surface flux and
579 investigate whether the multi-scale interaction mechanism would collaborate with the convection-
580 radiation-surface flux feedback mechanisms.

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588 **References**

- 589 Back, A., and J. A. Biello, 2018: Effect of overturning circulation on long equatorial waves: A
590 low-frequency cutoff. *J. Atmos. Sci.*, **75** (5), 1721–1739.
- 591 Biello, J. A., and A. J. Majda, 2010: Intraseasonal multi-scale moist dynamics of the tropical
592 atmosphere. *Communications in Mathematical Sciences*, **8** (2), 519–540.
- 593 Brenowitz, N., A. Majda, and Q. Yang, 2018: The multiscale impacts of organized convection in
594 global 2-d cloud-resolving models. *JAMES*, **10** (8), 2009–2025.
- 595 Bretherton, C. S., P. N. Blossey, and M. Khairoutdinov, 2005: An energy-balance analysis of deep
596 convective self-aggregation above uniform sst. *J. Atmos. Sci.*, **62** (12), 4273–4292.
- 597 Bretherton, C. S., and M. F. Khairoutdinov, 2015: Convective self-aggregation feedbacks in near-
598 global cloud-resolving simulations of an aquaplanet. *JAMES*, **7** (4), 1765–1787.
- 599 Chen, S. S., R. A. Houze, Jr., and B. E. Mapes, 1996: Multiscale variability of deep convection in
600 relation to large-scale circulation in TOGA COARE. *J. Atmos. Sci.*, **53** (10), 1380–1409.
- 601 Deng, Q., B. Khouider, and A. J. Majda, 2015: The MJO in a coarse-resolution gcm with a
602 stochastic multicloud parameterization. *J. Atmos. Sci.*, **72** (1), 55–74.
- 603 Gadgil, S., 2003: The indian monsoon and its variability. *Annual Review of Earth and Planetary
604 Sciences*, **31** (1), 429–467.

- 605 Goswami, B., B. Khouider, R. Phani, P. Mukhopadhyay, and A. J. Majda, 2017: Improving synop-
606 tic and intra-seasonal variability in CFSv2 via stochastic representation of organized convection.
607 *Geophys. Res. Lett.*, **44** (2), 1104–1113.
- 608 Grabowski, W. W., and M. W. Moncrieff, 2001: Large-scale organization of tropical convection
609 in two-dimensional explicit numerical simulations. *Quart. J. Roy. Meteor. Soc.*, **127** (572), 445–
610 468.
- 611 Guichard, F., and F. Couvreux, 2017: A short review of numerical cloud-resolving models. *Tellus*
612 *A: Dynamic Meteorology and Oceanography*, **69** (1), 1373 578.
- 613 Guo, Y., D. E. Waliser, and X. Jiang, 2015: A systematic relationship between the representations
614 of convectively coupled equatorial wave activity and the madden–julian oscillation in climate
615 model simulations. *JCLI*, **28** (5), 1881–1904.
- 616 Held, I. M., R. S. Hemler, and V. Ramaswamy, 1993: Radiative-convective equilibrium with ex-
617 plicit two-dimensional moist convection. *J. Atmos. Sci.*, **50** (23), 3909–3927.
- 618 Houze, R. A., Jr., 2004: Mesoscale convective systems. *Rev. Geophys.*, **42** (4).
- 619 Hurley, J. V., and W. R. Boos, 2015: A global climatology of monsoon low-pressure systems.
620 *Quart. J. Roy. Meteor. Soc.*, **141** (689), 1049–1064.
- 621 Jiang, X., and Coauthors, 2015: Vertical structure and physical processes of the Madden-Julian
622 oscillation: Exploring key model physics in climate simulations. *Journal of Geophysical Re-*
623 *search: Atmospheres*, **120** (10), 4718–4748.
- 624 Khairoutdinov, M. F., and D. A. Randall, 2003: Cloud resolving modeling of the arm summer
625 1997 iop: Model formulation, results, uncertainties, and sensitivities. *J. Atmos. Sci.*, **60** (4),
626 607–625.

- 627 Khouider, B., J. Biello, and A. J. Majda, 2010: A stochastic multicloud model for tropical convec-
628 *tion. Communications in Mathematical Sciences*, **8** (1), 187–216.
- 629 Khouider, B., and A. J. Majda, 2006a: Model multi-cloud parameterizations for convectively
630 coupled waves: Detailed nonlinear wave evolution. *Dyn. Atmos. Oceans*, **42** (1), 59–80.
- 631 Khouider, B., and A. J. Majda, 2006b: Multicloud convective parametrizations with crude vertical
632 structure. *Theor. Comput. Fluid Dyn.*, **20** (5-6), 351–375.
- 633 Khouider, B., and A. J. Majda, 2006c: A simple multicloud parameterization for convectively
634 coupled tropical waves. part I: Linear analysis. *J. Atmos. Sci.*, **63** (4), 1308–1323.
- 635 Khouider, B., and A. J. Majda, 2007: A simple multicloud parameterization for convectively
636 coupled tropical waves. part II: Nonlinear simulations. *J. Atmos. Sci.*, **64** (2), 381–400.
- 637 Khouider, B., and A. J. Majda, 2008a: Equatorial convectively coupled waves in a simple multi-
638 cloud model. *J. Atmos. Sci.*, **65** (11), 3376–3397.
- 639 Khouider, B., and A. J. Majda, 2008b: Multicloud models for organized tropical convection:
640 Enhanced congestus heating. *J. Atmos. Sci.*, **65** (3), 895–914.
- 641 Kiladis, G. N., M. C. Wheeler, P. T. Haertel, K. H. Straub, and P. E. Roundy, 2009: Convectively
642 coupled equatorial waves. *Rev. Geophys.*, **47** (2).
- 643 Kim, H., F. Vitart, and D. E. Waliser, 2018: Prediction of the madden–julian oscillation: A review.
644 *J. Climate*, **31** (23), 9425–9443.
- 645 Liu, C., and M. W. Moncrieff, 2004: Effects of convectively generated gravity waves and rotation
646 on the organization of convection. *J. Atmos. Sci.*, **61** (17), 2218–2227.

- 647 Majda, A. J., 2000: Real world turbulence and modern applied mathematics. *Mathematics: frontiers and perspectives*, 137–151.
- 648
- 649 Majda, A. J., 2007: New multiscale models and self-similarity in tropical convection. *J. Atmos. Sci.*, **64** (4), 1393–1404.
- 650
- 651 Majda, A. J., 2012: Climate science, waves and pdes for the tropics. *Nonlinear Partial Differential Equations*, Springer, 223–230.
- 652
- 653 Majda, A. J., B. Khouider, and Y. Frenkel, 2015: Effects of rotation and mid-troposphere moisture on organized convection and convectively coupled gravity waves. *Climate Dyn.*, **44** (3-4), 937–960.
- 654
- 655
- 656 Majda, A. J., and R. Klein, 2003: Systematic multiscale models for the tropics. *J. Atmos. Sci.*, **60** (2), 393–408.
- 657
- 658 Majda, A. J., M. Mohammadian, and Y. Xing, 2008: Vertically sheared horizontal flow with mass sources: a canonical balanced model. *Geophysical and Astrophysical Fluid Dynamics*, **102** (6), 543–591.
- 659
- 660
- 661 Majda, A. J., and Q. Yang, 2016: A multiscale model for the intraseasonal impact of the diurnal cycle over the maritime continent on the Madden–Julian oscillation. *J. Atmos. Sci.*, **73** (2), 579–604.
- 662
- 663
- 664 Miura, H., M. Satoh, T. Nasuno, A. T. Noda, and K. Oouchi, 2007: A Madden-Julian oscillation event realistically simulated by a global cloud-resolving model. *Science*, **318** (5857), 1763–1765.
- 665
- 666
- 667 Moncrieff, M., 1981: A theory of organized steady convection and its transport properties. *Quart. J. Roy. Meteor. Soc.*, **107**, 29–50.
- 668

- 669 Moncrieff, M. W., and C. Liu, 1999: Convection initiation by density currents: Role of conver-
670 gence, shear, and dynamical organization. *Mon. Wea. Rev.*, **127** (10), 2455–2464.
- 671 Moncrieff, M. W., C. Liu, and P. Bogenschutz, 2017: Simulation, modeling, and dynamically
672 based parameterization of organized tropical convection for global climate models. *J. Atmos.*
673 *Sci.*, **74** (5), 1363–1380.
- 674 Muller, C. J., and I. M. Held, 2012: Detailed investigation of the self-aggregation of convection in
675 cloud-resolving simulations. *J. Atmos. Sci.*, **69** (8), 2551–2565.
- 676 Nakazawa, T., 1988: Tropical super clusters within intraseasonal variations over the western pa-
677 cific. *J. Meteor. Soc. Japan*, **66** (6), 823–839.
- 678 Newton, C. W., and H. Rodebush Newton, 1959: Dynamical interactions between large convective
679 clouds and environment with vertical shear. *J. Meteor.*, **16** (5), 483–496.
- 680 Riemann-Campe, K., K. Fraedrich, and F. Lunkeit, 2009: Global climatology of convective avail-
681 able potential energy (cape) and convective inhibition (cin) in era-40 reanalysis. *Atmos. Res.*,
682 **93** (1-3), 534–545.
- 683 Schneider, T., 2006: The general circulation of the atmosphere. *Annu. Rev. Earth Planet. Sci.*, **34**,
684 655–688.
- 685 Slawinska, J., O. Pauluis, A. J. Majda, and W. W. Grabowski, 2014: Multiscale interactions in
686 an idealized walker circulation: Mean circulation and intraseasonal variability. *J. Atmos. Sci.*,
687 **71** (3), 953–971.
- 688 Tao, W.-K., and M. W. Moncrieff, 2009: Multiscale cloud system modeling. *Rev. Geophys.*, **47** (4).
- 689 Tompkins, A. M., 2001: Organization of tropical convection in low vertical wind shears: The role
690 of water vapor. *J. Atmos. Sci.*, **58** (6), 529–545.

- 691 Vallis, G. K., 2017: *Atmospheric and oceanic fluid dynamics*. Cambridge University Press.
- 692 Waliser, D. E., and C. Gautier, 1993: A satellite-derived climatology of the ITCZ. *J. Climate*,
693 **6** (11), 2162–2174.
- 694 Wing, A. A., and T. W. Cronin, 2016: Self-aggregation of convection in long channel geometry.
695 *Quart. J. Roy. Meteor. Soc.*, **142** (694), 1–15.
- 696 Wing, A. A., and K. A. Emanuel, 2014: Physical mechanisms controlling self-aggregation of
697 convection in idealized numerical modeling simulations. *JAMES*, **6** (1), 59–74.
- 698 Yang, Q., and A. J. Majda, 2014: A multi-scale model for the intraseasonal impact of the diurnal
699 cycle of tropical convection. *Theor. Comput. Fluid Dyn.*, **28** (6), 605–633.
- 700 Yang, Q., and A. J. Majda, 2017: Upscale impact of mesoscale disturbances of tropical convection
701 on synoptic-scale equatorial waves in two-dimensional flows. *J. Atmos. Sci.*, **74** (9), 3099–3120.
- 702 Yang, Q., and A. J. Majda, 2018: Upscale impact of mesoscale disturbances of tropical convection
703 on convectively coupled kelvin waves. *J. Atmos. Sci.*, **75** (1), 85–111.
- 704 Yang, Q., and A. J. Majda, 2019: Upscale impact of mesoscale disturbances of tropical convection
705 on 2-day waves. *J. Atmos. Sci.*, **76** (1), 171–194.
- 706 Yang, Q., A. J. Majda, and B. Khouider, 2017: ITCZ breakdown and its upscale impact on the
707 planetary-scale circulation over the eastern pacific. *J. Atmos. Sci.*, **74** (12), 4023–4045.
- 708 Yang, Q., A. J. Majda, and M. W. Moncrieff, 2019: Upscale impact of mesoscale convective sys-
709 tems and its parameterization in an idealized gcm for a mjo analog above the equator. *accepted*
710 by *Journal of the Atmospheric Sciences*.
- 711 Zhang, C., 2005: Madden-Julian oscillation. *Rev. Geophys.*, **43** (2).

712 LIST OF TABLES

713	Table 1.	Coriolis force parameter ($f = 2\Omega \sin(\phi)$) and the corresponding time scale ($\frac{1}{f}$) in these 10 cases.	35
714			
715	Table 2.	Multi-scale asymptotic model across planetary-, synoptic- and meso-scales in the weak rotation regime.	36
716			
717	Table 3.	Multi-scale asymptotic model across planetary-, synoptic- and meso-scales in the order-one rotation regime.	37
718			
719	Table 4.	Multi-scale asymptotic model across planetary-, synoptic- and meso-scales in the strong rotation regime.	38
720			

TABLE 1: Coriolis force parameter ($f = 2\Omega \sin(\phi)$) and the corresponding time scale ($\frac{1}{f}$) in these 10 cases.

Regime	Latitude (deg N)	Coriolis f (1/s)	$\frac{1}{f}$ (hrs)
No Rotation	0	0	∞
Weak Rotation	1	2.5×10^{-6}	109.1
	3	7.6×10^{-6}	36.4
	5	1.3×10^{-5}	21.9
Order-One Rotation	9	2.3×10^{-5}	12.2
	14	3.5×10^{-5}	7.9
	20	5.0×10^{-5}	5.6
Strong Rotation	27	6.6×10^{-5}	4.2
	35	8.4×10^{-5}	3.3
	45	1.0×10^{-4}	2.7

TABLE 2: Multi-scale asymptotic model across planetary-, synoptic- and meso-scales in the weak rotation regime.

Regime 1: Weak Rotation (\hat{f} from $\mathcal{O}(\varepsilon)$)		
Space and Time Scales	Governing Equations	Variables
Trade winds (planetary / intraseasonal)	$\frac{DU}{DT} = -P_X - \hat{d}(U - U_0)$ $\frac{D\Theta}{DT} + N^2 W = -\hat{d}_\theta \Theta + S_\theta$ $P_z = \Theta$ $U_X + \rho_0^{-1} (\rho_0 W)_z = 0$ $\frac{DQ}{DT} - Q_0 W = -S_\theta$	\hat{d}, \hat{d}_θ from $\mathcal{O}(\varepsilon)$ $\frac{D}{DT} = \frac{\partial}{\partial T} + U \frac{\partial}{\partial X} + W \frac{\partial}{\partial z}$ U, P, Θ, Q from $\mathcal{O}(1)$ V, W, S_θ from $\mathcal{O}(\varepsilon)$ $\rho_0 = \rho_0(z)$
Planetary / intraseasonal anomalies from the climatology	$\frac{Du}{DT} + u U_X + w U_z - \hat{f} V = -p_X - \hat{d} u$ $-\rho_0^{-1} (\rho_0 \langle \bar{w^* u^*} \rangle^p)_z - \rho_0^{-1} (\rho_0 \langle \bar{w' u'} \rangle^p)_z$ $\frac{DV}{DT} + \hat{f} u = -\hat{d} V$ $-\rho_0^{-1} (\rho_0 \langle \bar{w^* v^*} \rangle^p)_z - \rho_0^{-1} (\rho_0 \langle \bar{w' v'} \rangle^p)_z$ $\frac{D\theta}{DT} + u \Theta_X + w \Theta_z + N^2 w = -\hat{d}_\theta \theta + s_\theta$ $-\rho_0^{-1} (\rho_0 \langle \bar{w^* \theta^*} \rangle^p)_z - \rho_0^{-1} (\rho_0 \langle \bar{w' \theta'} \rangle^p)_z$ $p_z = \theta$ $u_X + \rho_0^{-1} (\rho_0 w)_z = 0$ $\frac{Dq}{DT} + u Q_X + w Q_z - Q_0 w = -s_\theta$ $-\rho_0^{-1} (\rho_0 \langle \bar{w^* q^*} \rangle^p)_z - \rho_0^{-1} (\rho_0 \langle \bar{w' q'} \rangle^p)_z$	$N^2 = 1$ u, V, p, θ, q from $\mathcal{O}(\varepsilon)$ w, s_θ from $\mathcal{O}(\varepsilon^2)$
Synoptic fluctuations in space or time	$u_t^* + U u_x^* + w^* U_z = -p_x^* - \rho_0^{-1} (\rho_0 \langle \bar{w' u'} \rangle^s)_z$ $v_t^* + U v_x^* = -\rho_0^{-1} (\rho_0 \langle \bar{w' v'} \rangle^s)_z$ $\theta_t^* + U \theta_x^* + w^* \Theta_z + N^2 w^* = -\rho_0^{-1} (\rho_0 \langle \bar{w' \theta'} \rangle^s)_z + s_\theta^*$ $p_z^* = \theta^*$ $u_x^* + \rho_0^{-1} (\rho_0 w^*)_z = 0$ $q_t^* + U q_x^* + w^* Q_z - Q_0 w^* = -s_\theta^* - \rho_0^{-1} (\rho_0 \langle \bar{w' q'} \rangle^s)_z$	all variables from $\mathcal{O}(\varepsilon)$
Mesoscale fluctuations in space and time	$u'_\tau + U u'_{x'} + w' U_z = -p'_{x'}$ $v'_\tau + U v'_{x'} = 0$ $\theta'_\tau + U \theta'_{x'} + w' \Theta_z + N^2 w' = s'_\theta$ $p'_z = \theta'$ $u'_{x'} + \rho_0^{-1} (\rho_0 w')_z = 0$ $q'_\tau + U q'_{x'} + w' Q_z - Q_0 w' = -s'_\theta$	u', v', p', θ', q' from $\mathcal{O}(\varepsilon)$ w', s'_θ from $\mathcal{O}(1)$

TABLE 3: Multi-scale asymptotic model across planetary-, synoptic- and meso-scales in the order-one rotation regime.

Regime 2: Order-One Rotation (\hat{f} from $\mathcal{O}(1)$)		
Space and Time Scales	Governing Equations	Variables
Trade winds (planetary / intraseasonal)	$\frac{DU}{DT} - \hat{f}V = -P_X - \hat{d}(U - U_0)$ $\hat{f}U = -\varepsilon^2 \hat{d}V$ $\frac{D\Theta}{DT} + N^2 W = -\hat{d}_\theta \Theta + S_\theta$ $P_z = \Theta$ $U_X + \rho_0^{-1} (\rho_0 W)_z = 0$ $\frac{DQ}{DT} - Q_0 W = -S_\theta$	\hat{d}, \hat{d}_θ from $\mathcal{O}(\varepsilon)$ $\frac{D}{DT} = \frac{\partial}{\partial T} + U \frac{\partial}{\partial X} + W \frac{\partial}{\partial z}$ U, P, Θ, Q from $\mathcal{O}(1)$ V, W, S_θ from $\mathcal{O}(\varepsilon)$
Planetary / intraseasonal anomalies from the climatology	$\frac{Du}{DT} + uU_X + wU_z - \hat{f}v = -p_X - \hat{d}u$ $-\rho_0^{-1} (\rho_0 \langle \bar{w^* u^*} \rangle^p)_z - \rho_0^{-1} (\rho_0 \langle \bar{w' u'} \rangle^p)_z$ $\hat{f}u = -\varepsilon^2 \hat{d}v$ $\frac{D\theta}{DT} + u\Theta_X + w\Theta_z + N^2 w = -\hat{d}_\theta \theta + s_\theta$ $-\rho_0^{-1} (\rho_0 \langle \bar{w^* \theta^*} \rangle^p)_z - \rho_0^{-1} (\rho_0 \langle \bar{w' \theta'} \rangle^p)_z$ $p_z = \theta$ $u_X + \rho_0^{-1} (\rho_0 w)_z = 0$ $\frac{Dq}{DT} + uQ_X + wQ_z - Q_0 w = -s_\theta$ $-\rho_0^{-1} (\rho_0 \langle \bar{w^* q^*} \rangle^p)_z - \rho_0^{-1} (\rho_0 \langle \bar{w' q'} \rangle^p)_z$	$N^2 = 1$ u, p, θ, q from $\mathcal{O}(\varepsilon)$ v, w, s_θ from $\mathcal{O}(\varepsilon^2)$
Synoptic fluctuations in space or time	$u_t^* + U u_x^* + w^* U_z - \hat{f}v^* = -p_x^* - \rho_0^{-1} (\rho_0 \langle \bar{w' u'} \rangle^s)_z$ $v_t^* + U v_x^* + \hat{f}u^* = -\rho_0^{-1} (\rho_0 \langle \bar{w' v'} \rangle^s)_z$ $\theta_t^* + U \theta_x^* + w^* \Theta_z + N^2 w^* = -\rho_0^{-1} (\rho_0 \langle \bar{w' \theta'} \rangle^s)_z + s_\theta^*$ $p_z^* = \theta^*$ $u_x^* + \rho_0^{-1} (\rho_0 w^*)_z = 0$ $q_t^* + U q_x^* + w^* Q_z - Q_0 w^* = -s_\theta^* - \rho_0^{-1} (\rho_0 \langle \bar{w' q'} \rangle^s)_z$	all variables from $\mathcal{O}(\varepsilon)$
Mesoscale fluctuations in space and time	$u'_\tau + U u'_{x'} + w' U_z = -p'_{x'}$ $v'_\tau + U v'_{x'} = 0$ $\theta'_\tau + U \theta'_{x'} + w' \Theta_z + N^2 w' = s'_\theta$ $p'_z = \theta'$ $u'_{x'} + \rho_0^{-1} (\rho_0 w')_z = 0$ $q'_\tau + U q'_{x'} + w' Q_z - Q_0 w' = -s_\theta'$	u', v', p', θ', q' from $\mathcal{O}(\varepsilon)$ w', s'_θ from $\mathcal{O}(1)$

TABLE 4: Multi-scale asymptotic model across planetary-, synoptic- and meso-scales in the strong rotation regime.

Regime 3: Strong Rotation (\hat{f} from $\mathcal{O}(\varepsilon^{-1})$)		
Space and Time Scales	Governing Equations	Variables
Planetary / synoptic-time circulation	$U_t - \hat{f}V = -P_X - \hat{d}(U - U_0)$ $\hat{f}U = -\varepsilon^2 \hat{d}V$ $\Theta_t + N^2 W = S_\theta - \hat{d}_\theta \Theta$ $P_z = \Theta$ $U_X + \rho_0^{-1} (\rho_0 W)_z = 0$	\hat{d}, \hat{d}_θ from $\mathcal{O}(1)$ U, P, Θ, S_θ from $\mathcal{O}(1)$ V, W from $\mathcal{O}(\varepsilon)$
Synoptic fluctuations in QG regime	$\frac{D}{Dt} (\phi_{xx}^* + \hat{f}^2 \phi_{zz}^*) = -\hat{d}\phi_{xx}^* - \hat{d}_\theta \hat{f}^2 \phi_{zz}^* + \hat{f} (s_\theta^*)_z$	$\frac{D}{Dt} = \frac{\partial}{\partial t} + U \frac{\partial}{\partial x}$ $u^* = 0, v^* = \phi_x^*, \theta^* = \hat{f}\phi_z^*$ all variables from $\mathcal{O}(1)$
Mesoscale fluctuations in space and time	$u'_\tau + (U + u^*) u'_{x'} + w' (U + u^*)_z - \hat{f}v' = -(p')_{x'}$ $v'_\tau + (U + u^*) v'_{x'} + w' v_z^* + \hat{f}u' = 0$ $N^2 w' = s'_\theta$ $u'_{x'} + \rho_0^{-1} (\rho_0 w')_z = 0$	u', v' from $\mathcal{O}(\varepsilon)$ w' from $\mathcal{O}(1)$ p' from $\mathcal{O}(\varepsilon^2)$ s'_θ from $\mathcal{O}(\varepsilon^{-1})$

LIST OF FIGURES

- Fig. 9.** Schematic diagram explaining why planetary-scale kinetic energy of zonal winds diminishes as the rotation f increases in the weak rotation regime. Panel (a) shows acceleration/deceleration effects in the planetary-scale kinetic energy budget of both zonal and meridional winds, where bold (thin) arrows indicate the dominant (secondary) energy source/sink terms. The red up (blue down) arrow represents increasing (decreasing) in magnitude. Overall, the diminishment of planetary kinetic energy of zonal winds is due to i) increasing deceleration term involving the Coriolis force, and ii) decreasing acceleration term involving eddy zonal momentum transfer from mesoscale fluctuations. Panel (b) attributes the diminishment of mesoscale convective systems to the increasing low-level equivalent potential temperature and decreasing low-level vertical shear in the background sounding as the rotation f increases.

Fig. 10. Vertical profiles of climatological-mean (domain-mean and time-mean) eddy heat transfer from (a) mesoscale fluctuations, (b) synoptic fluctuations, (c) planetary fluctuations, and (d) total, based on the last 80-day model output in the weak rotation regime. The unit of eddy heat transfer is Ks^{-2}

Fig. 11. Vertical profiles of climatological-mean (domain-mean and time-mean) available potential energy source and sink terms, based on the last 80-day model output in the weak rotation regime. Panel (a) shows the term involving energy transfer between kinetic energy and available potential energy. Panels (b-c) show available potential energy source and sinks terms involving eddy heat transfer from (b) synoptic fluctuations, (c) mesoscale fluctuations. Potential temperature is rescaled by a constant, $\tilde{\theta} = \frac{g}{\theta} \theta$. The dimensional unit of all terms is $kgm^{-1}s^{-3}$

Fig. 12. Vertical profiles of climatological-mean (domain-mean and time-mean) eddy transfer of equivalent potential temperature from (a) mesoscale fluctuations, (b) synoptic fluctuations, (c) planetary fluctuations, and (d) total, based on the last 80-day model output in the weak rotation regime. The unit of eddy transfer of equivalent potential temperature is K/s

Fig. 13. Vertical profiles of climatological-mean (domain-mean and time-mean) synoptic-scale energy source and sink terms based on the last 80-day model output in the order-one rotation regime. Panels (a-d) show the terms involving (a) eddy zonal momentum transfer, (b) eddy meridional momentum transfer, (c) eddy heat transfer, (d) the Coriolis force. Panel (e-f) show the terms representing energy conversion between kinetic energy and available potential energy. The dimensional unit of all terms is $10^{-5}kgm^{-1}s^{-3}$

Fig. 14. Climatological-mean (zonal and vertical mean, and time-mean) total synoptic-scale kinetic energy source and sink terms for (a) zonal winds, (b) meridional winds, based on the last 80-day model output in the order-one rotation regime. The dimensional unit of all terms is $kgm^{-1}s^{-3}$. The y-axis limit in both panels are $1.1 \times 10^{-5}kg/m/s^3$

Fig. 15. Schematic diagram explaining the maintenance of synoptic organization of convection and its diminishment as the rotation further increases in the order-one rotation regime. This figure shows acceleration/deceleration effects in the synoptic-scale kinetic energy budget of both zonal and meridional winds, where bold (thin) arrows indicate the dominant (secondary) energy source/sink terms. The blue down arrow represents decreasing in magnitude. Overall, the diminishment of synoptic kinetic energy of zonal winds is due to decreasing acceleration term involving eddy zonal momentum transfer from mesoscale fluctuations. The explanation for the diminishment of mesoscale convective systems is the same as Fig.12, so it is not repeated here.

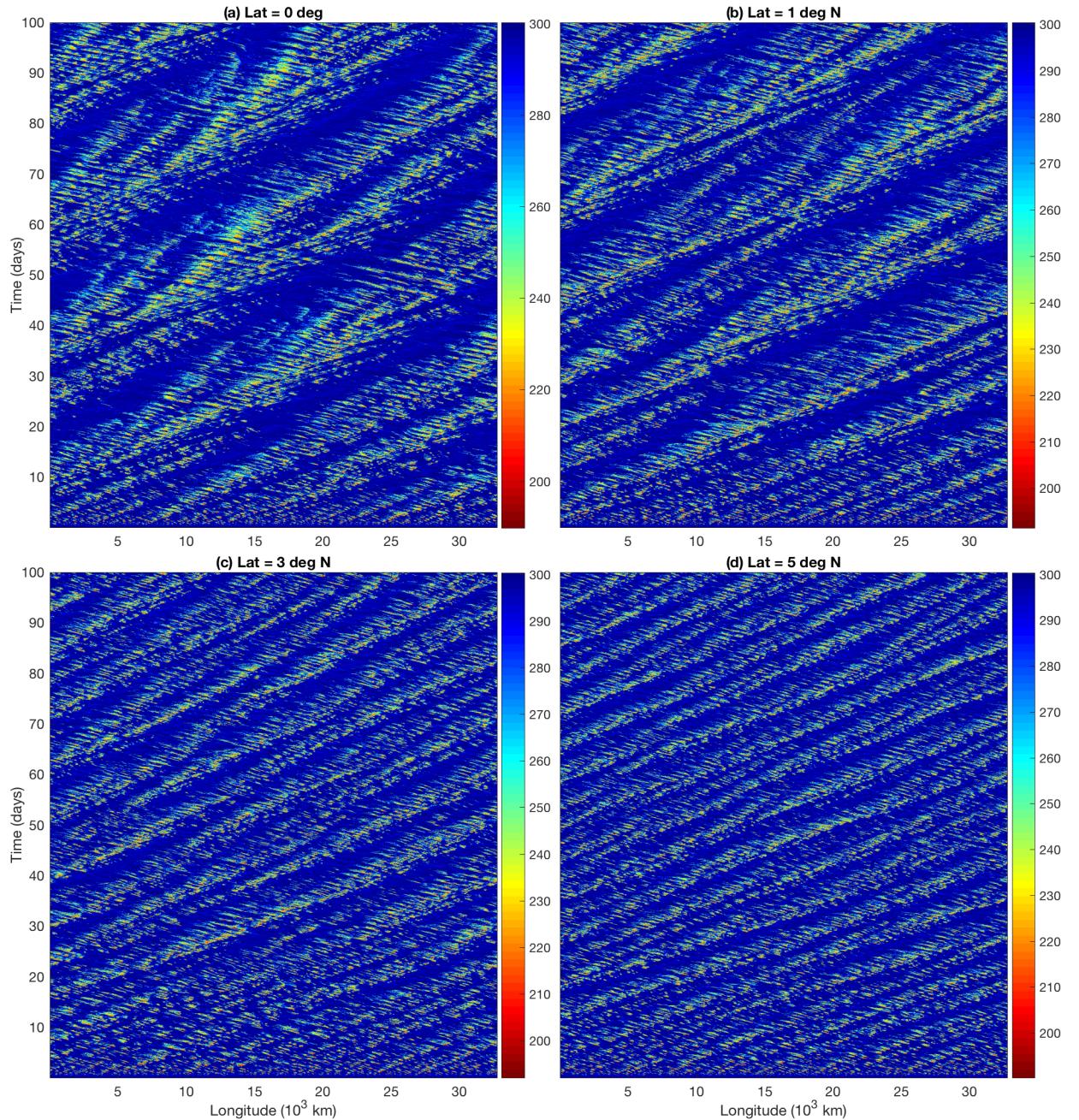


FIG. 1: Hovmöller diagrams of brightness temperature in cases with various magnitude of rotation. These panels correspond to the cases with f at the latitude (a) 0 deg, (b) 1 deg N, (c) 3 deg N, (d) 5 deg N, (e) 9 deg N, (f) 14 deg N, (g) 20 deg N, (h) 27 deg N. Depending on the magnitude of rotation, panels a-d, e-g, and h belong to the weak, order-one, and strong rotation regime, respectively. The output is coarse-grained into 16-km grid resolutions (averaged over every 8 x-grids). The unit is K.

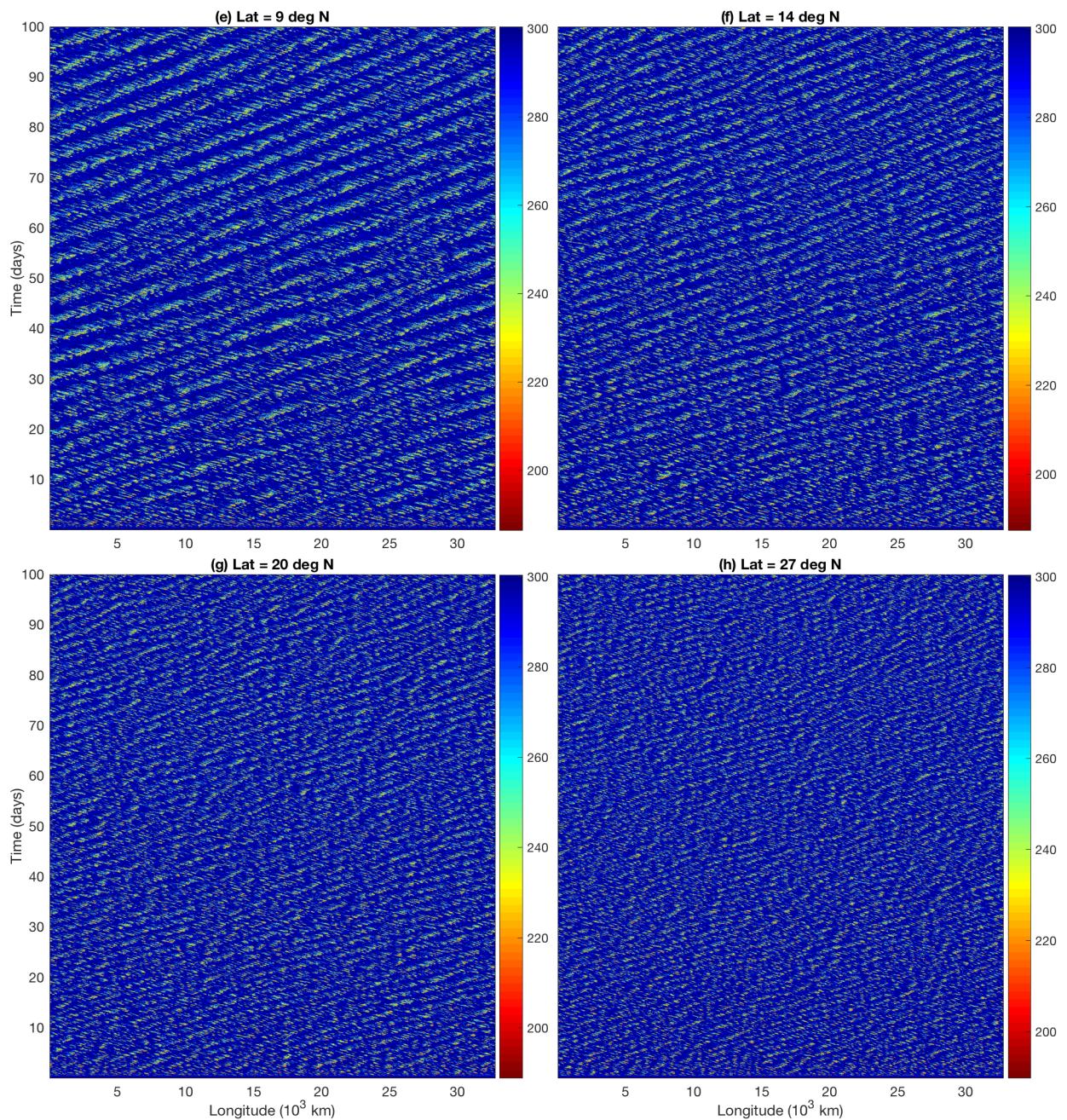


Fig. 1 continued.

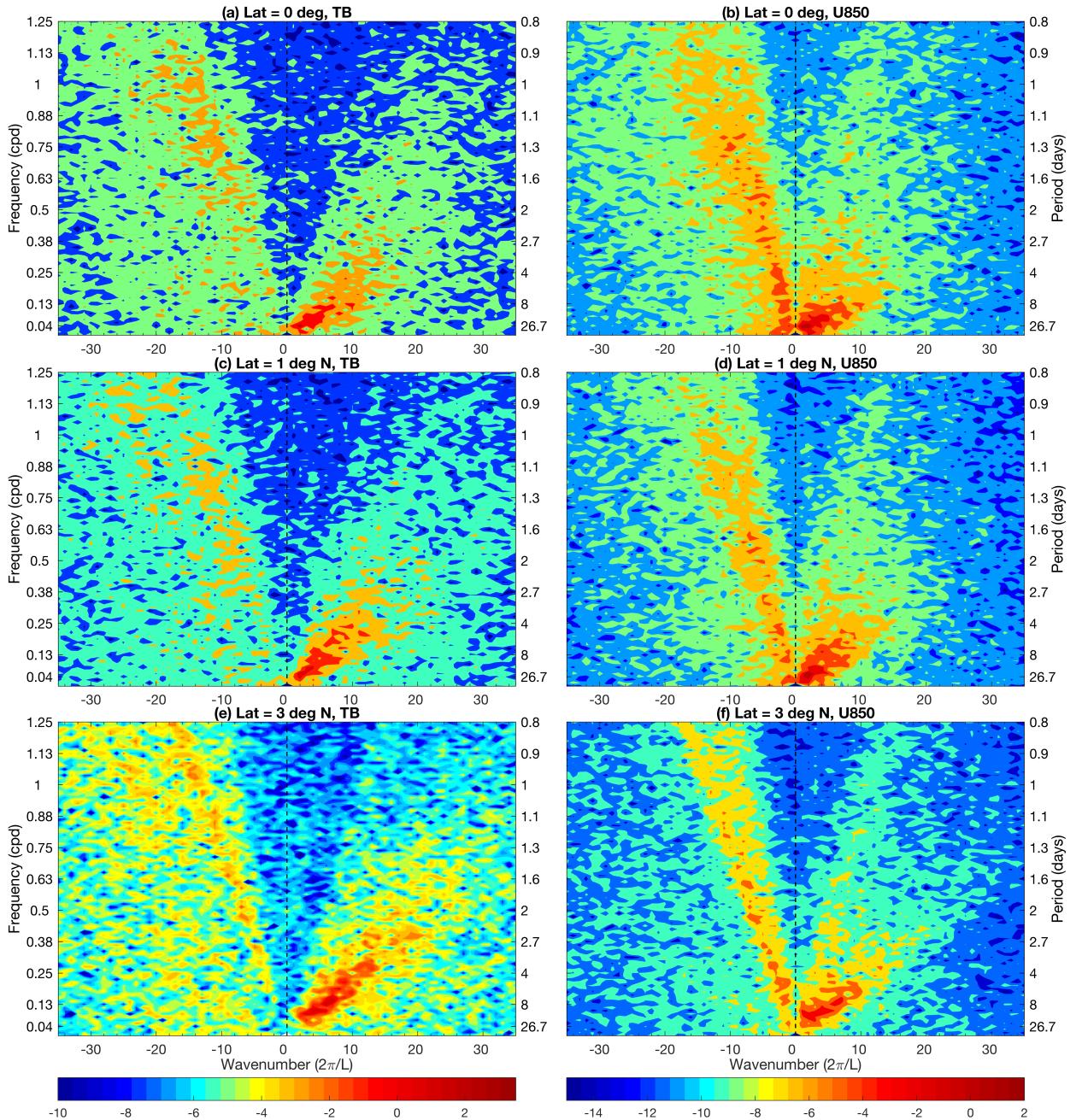


FIG. 2: Log-scale wavenumber-frequency spectra of brightness temperature (left) and 850-hPa zonal velocity (right) in cases with various magnitude of rotation based on the last 80-day output. These panels correspond the cases with f at the latitude (a,b) 0 deg, (c,d) 1 deg N, (e,f) 3 deg N, (g,h) 5 deg N, (i,j) 9 deg N, (k,l) 14 deg N, (m,n) 20 deg N, (o,p) 27 deg N, (q,r) 35 deg N. The value at the origin (zonal and time mean) is removed. The dimensional units of brightness temperature and zonal velocity is K and m/s, respectively.

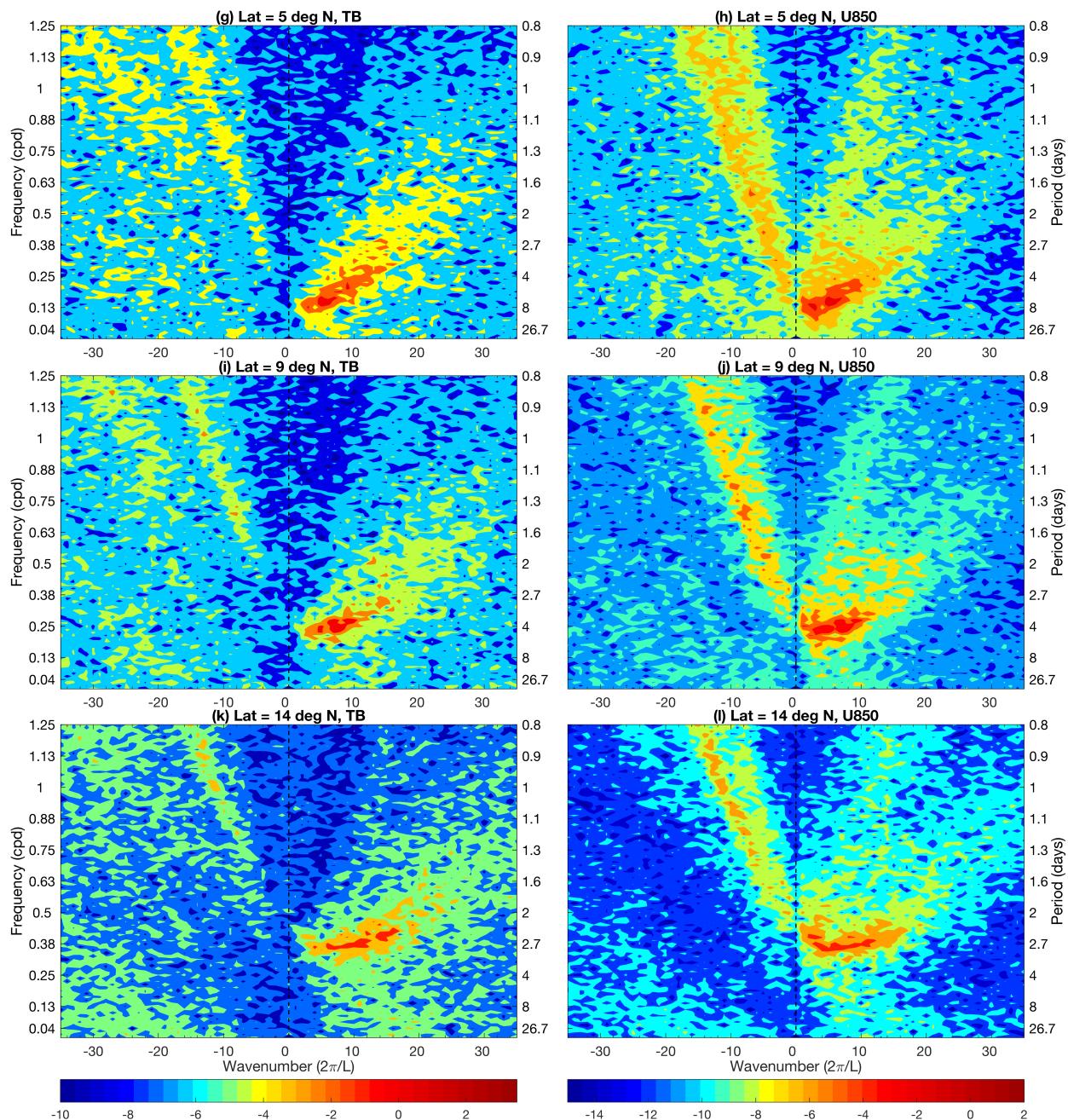


Fig. 2 continued.

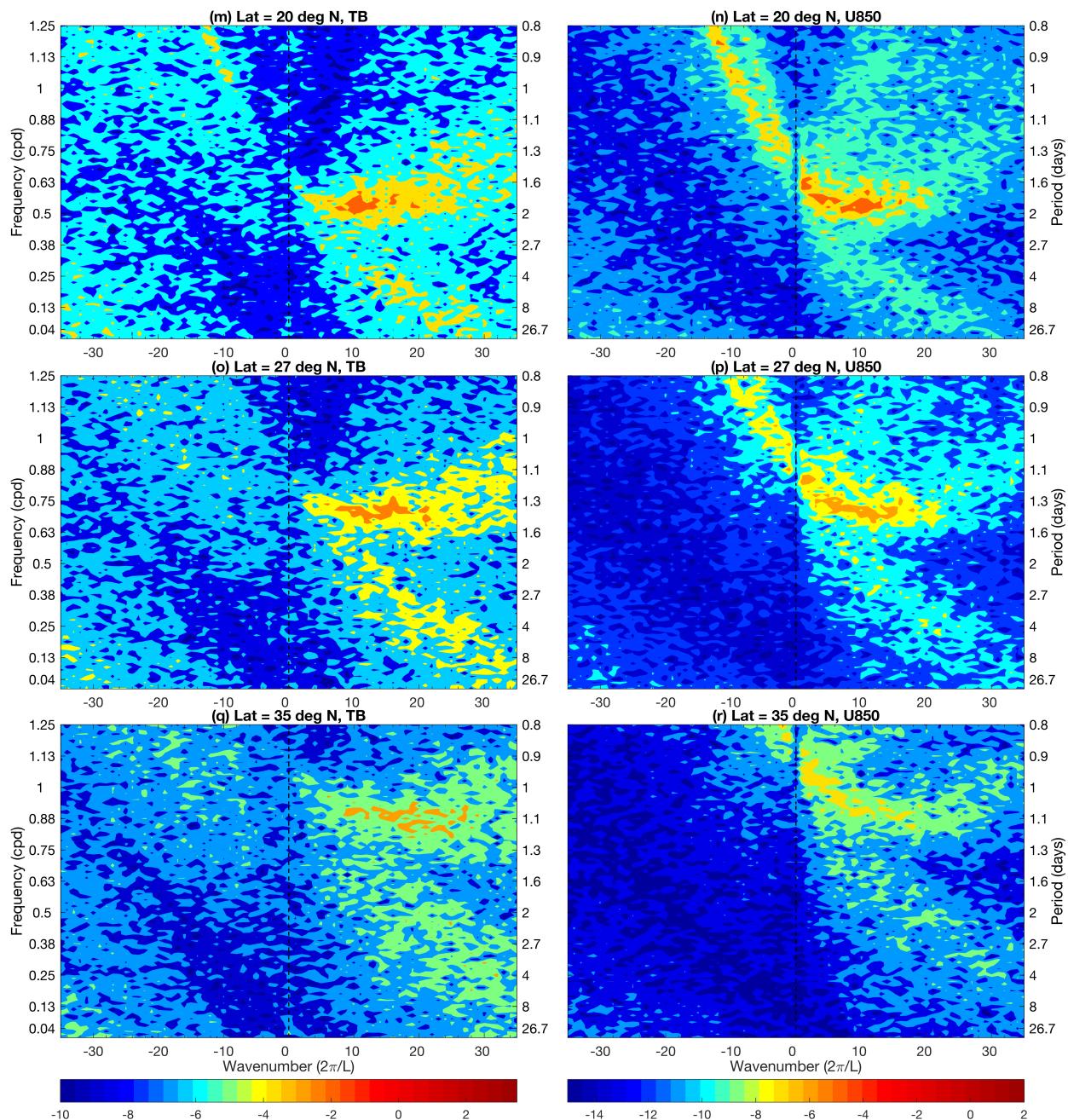


Figure 2 continued.

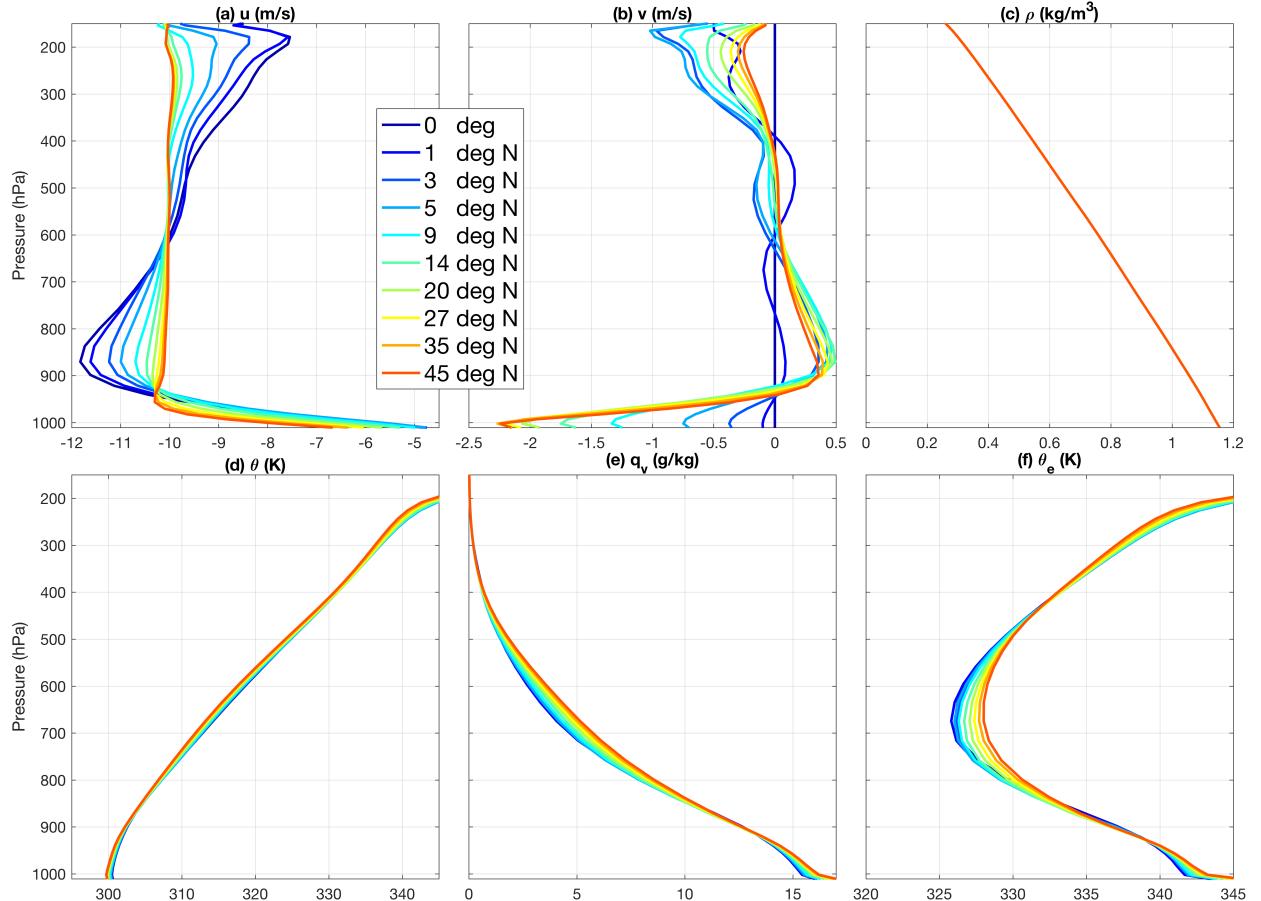


FIG. 3: Domain-mean climatology of (a) zonal velocity, (b) meridional velocity, (c), air density, (d) potential temperature, (e) water vapor, (f) equivalent potential temperature in these 10 cases based on last 80-day output. The horizontal axis shows the value of each field with its dimensional unit attached in the subtitle.

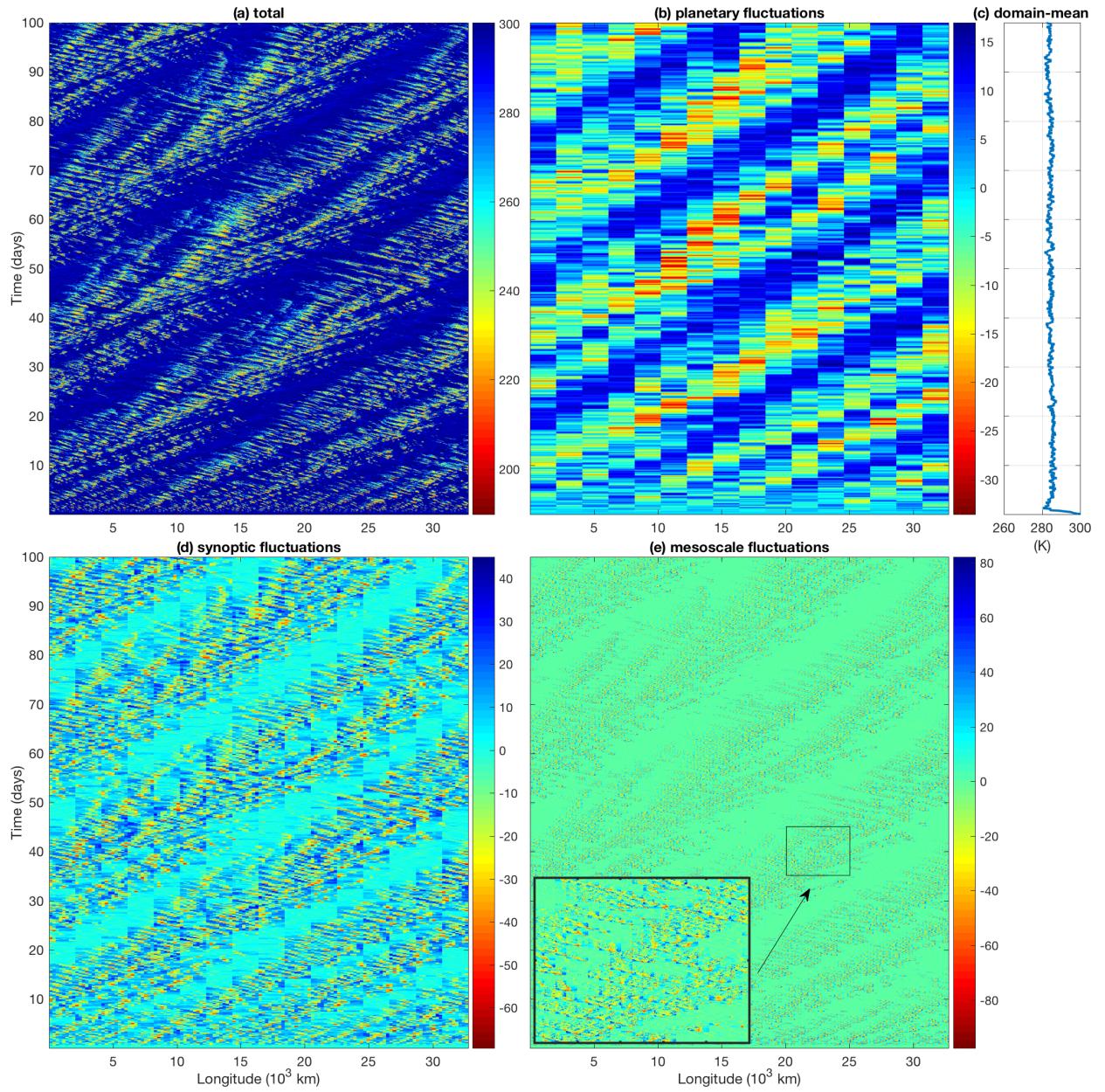


FIG. 4: Multi-scale decomposition of brightness temperature field in the non-rotating case through coarse graining method. Panel (a) shows the total field. Panels (b-d) show (b) planetary fluctuations, (c) domain-mean, (d) synoptic fluctuations, (e) mesoscale fluctuations. Coarse grid size in these panels is (a) 16 km, (b) 2048 km, (d) 256 km, (e) 16 km. The unit is K.

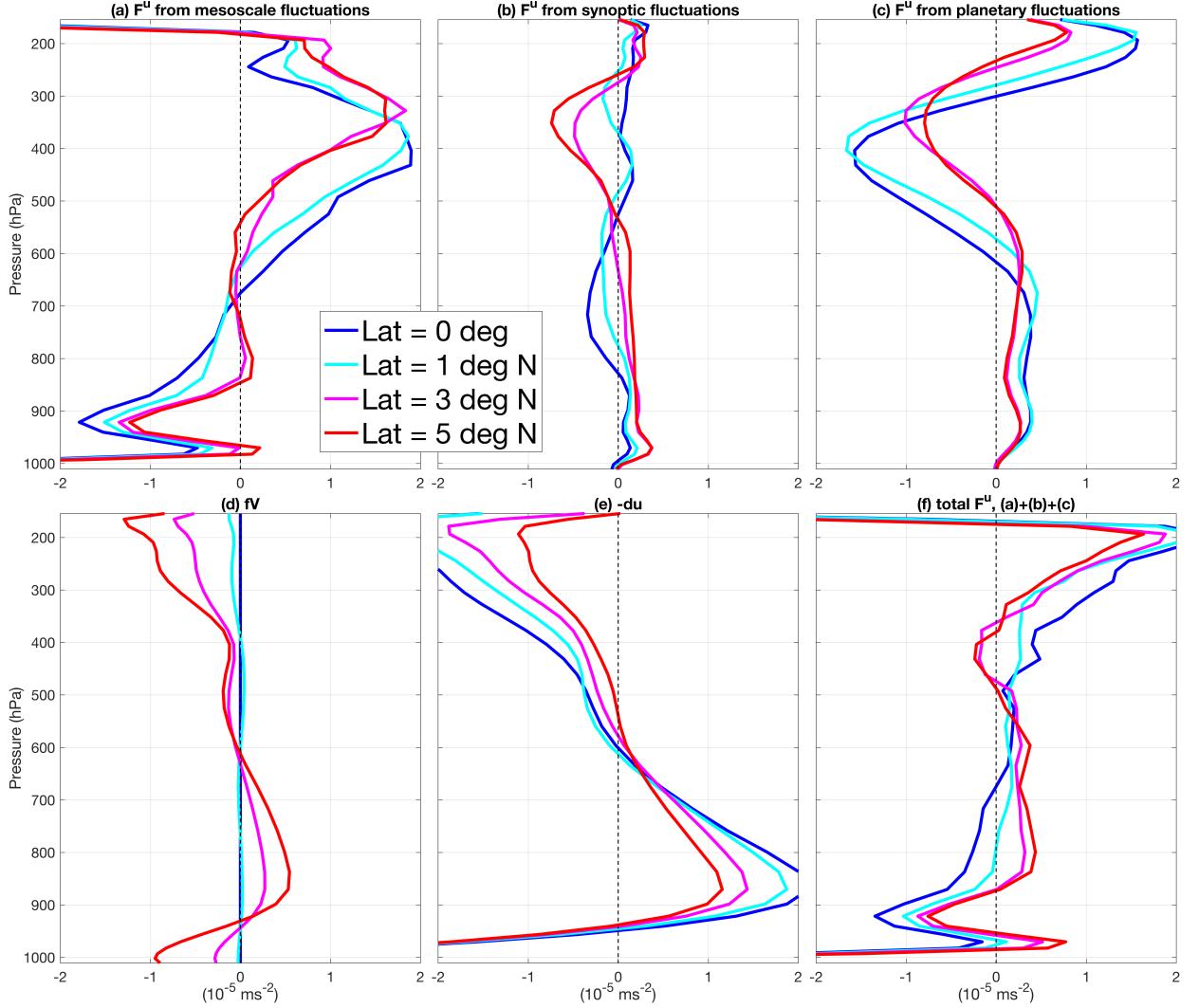


FIG. 5: Vertical profiles of climatological-mean (domain-mean and time-mean) zonal momentum budget terms based on the last 80-day model output in the weak rotation regime. Panels (a-c) show eddy zonal momentum transfer from (a) mesoscale fluctuations, (b) synoptic fluctuations, (c) planetary fluctuations, and panel (f) shows total. The remaining panels show (d) the Coriolis term, and (e) momentum damping. The unit of eddy zonal momentum transfer is ms^{-2} .

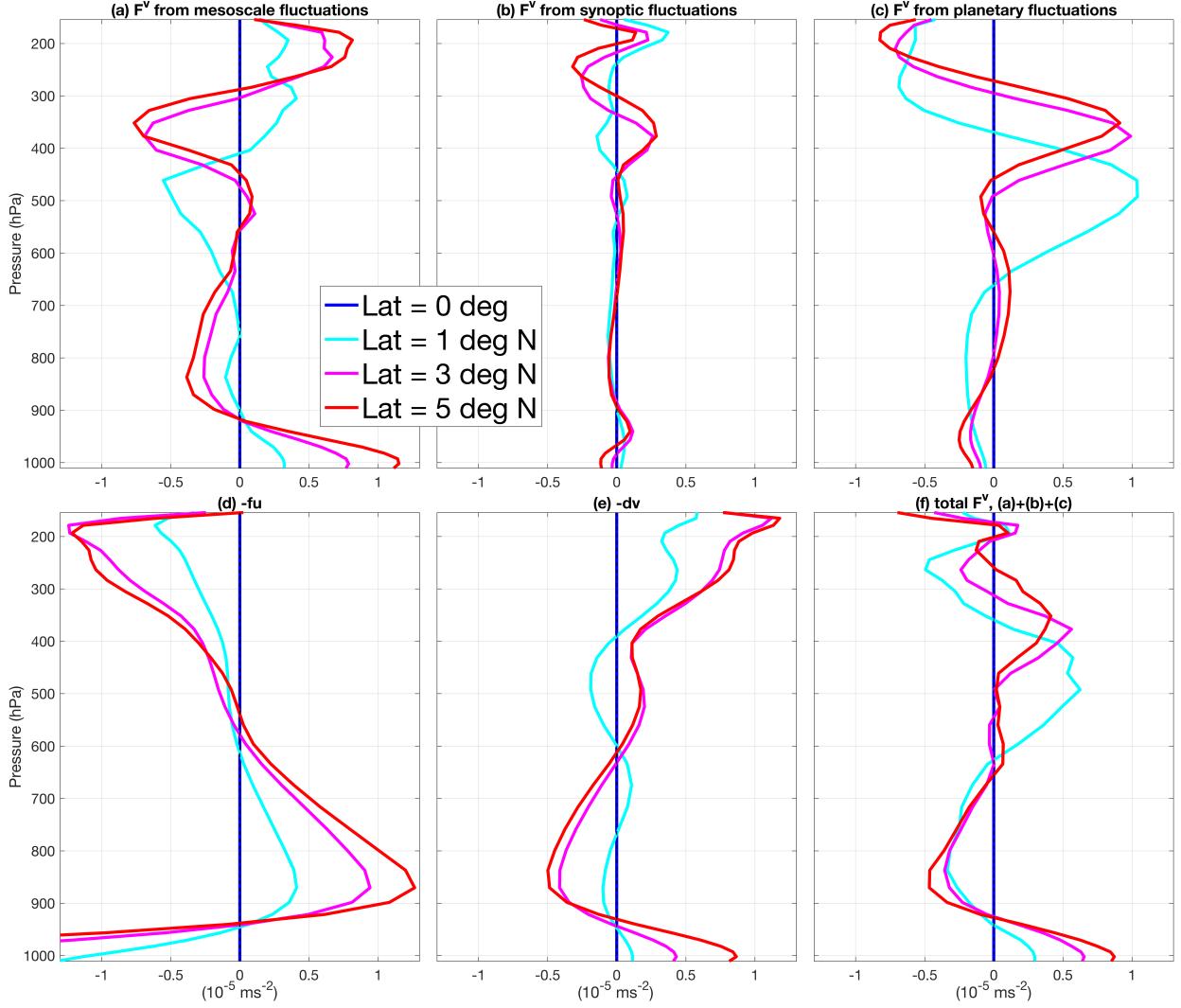


FIG. 6: Vertical profiles of climatological-mean (domain-mean and time-mean) meridional momentum budget terms based on the last 80-day model output in the weak rotation regime. Panels (a-c) show eddy meridional momentum transfer from (a) mesoscale fluctuations, (b) synoptic fluctuations, (c) planetary fluctuations, and panel (f) shows total. The remaining panels show (d) the Coriolis term, and (e) momentum damping. The unit of eddy meridional momentum transfer is ms^{-2} .

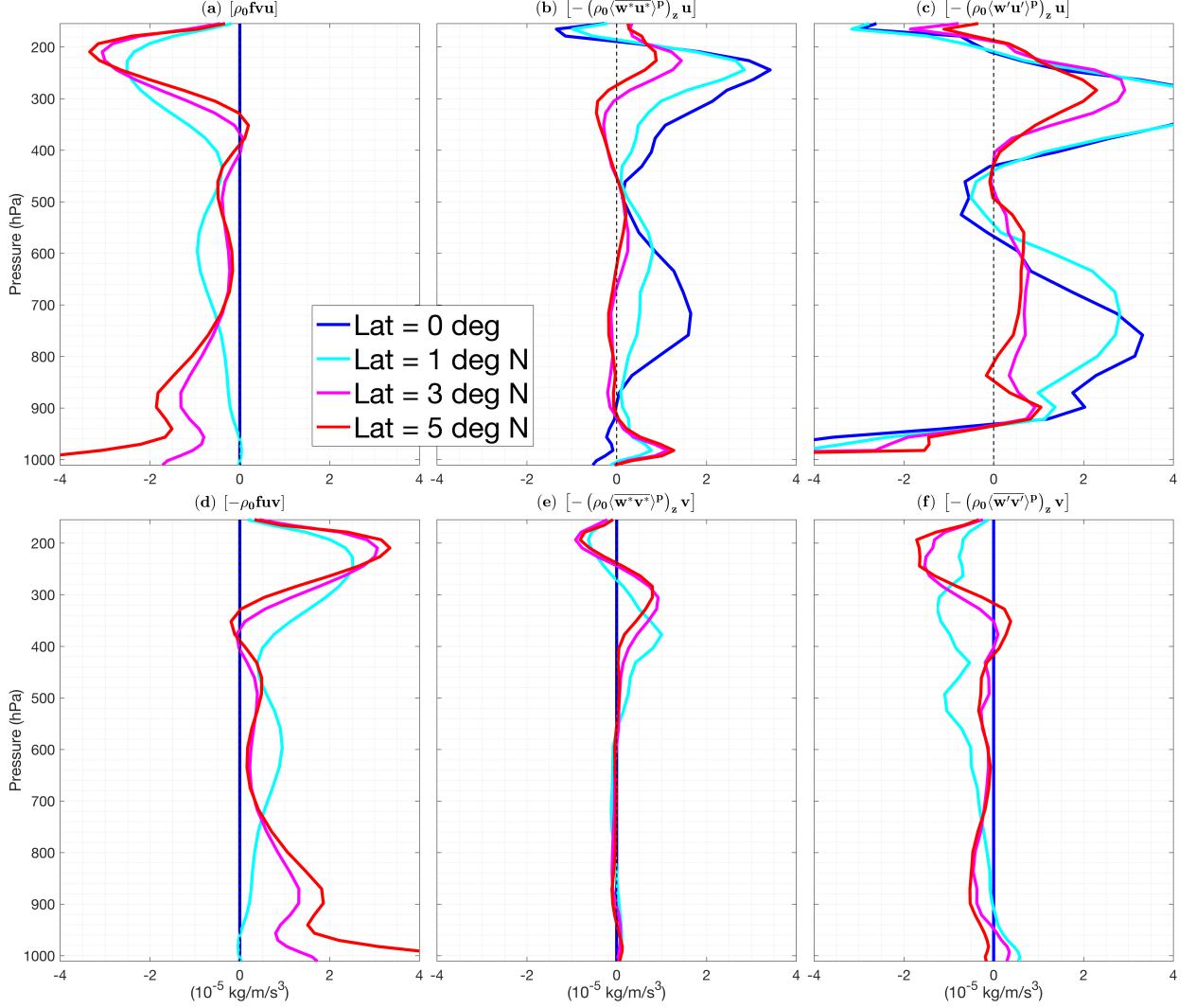


FIG. 7: Vertical profiles of climatological-mean (domain-mean and time-mean) planetary-scale kinetic energy source and sink terms, based on the last 80-day model output in the weak rotation regime. Panels (a-c) show the terms involving (a) the Coriolis force, (b) eddy zonal momentum transfer from synoptic fluctuations, (c) eddy zonal momentum transfer from mesoscale fluctuations. Panels (d-f) are similar to panels (a-c) but for meridional winds. The dimensional unit of all terms is $\text{kg m}^{-1} \text{s}^{-3}$.

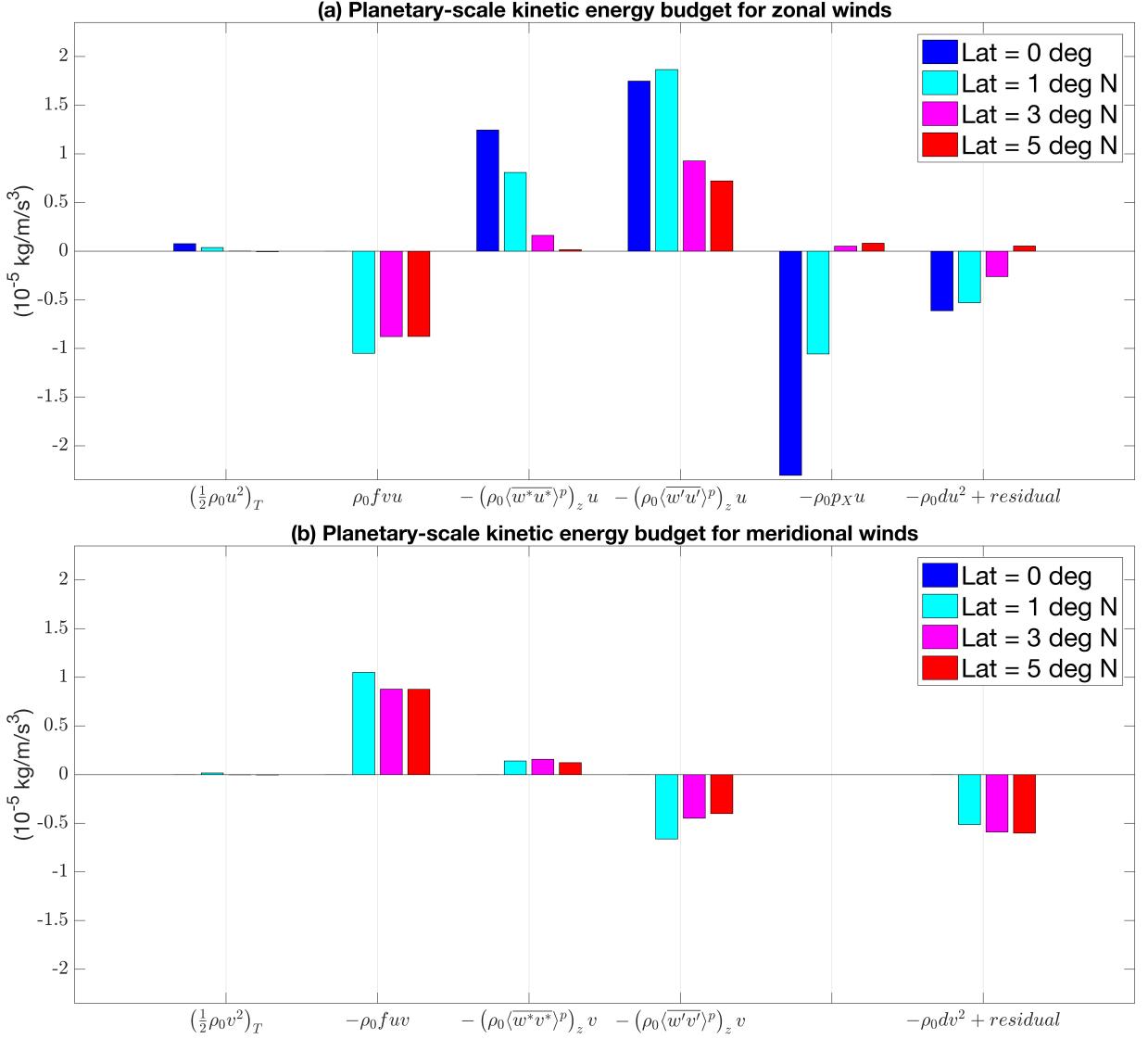
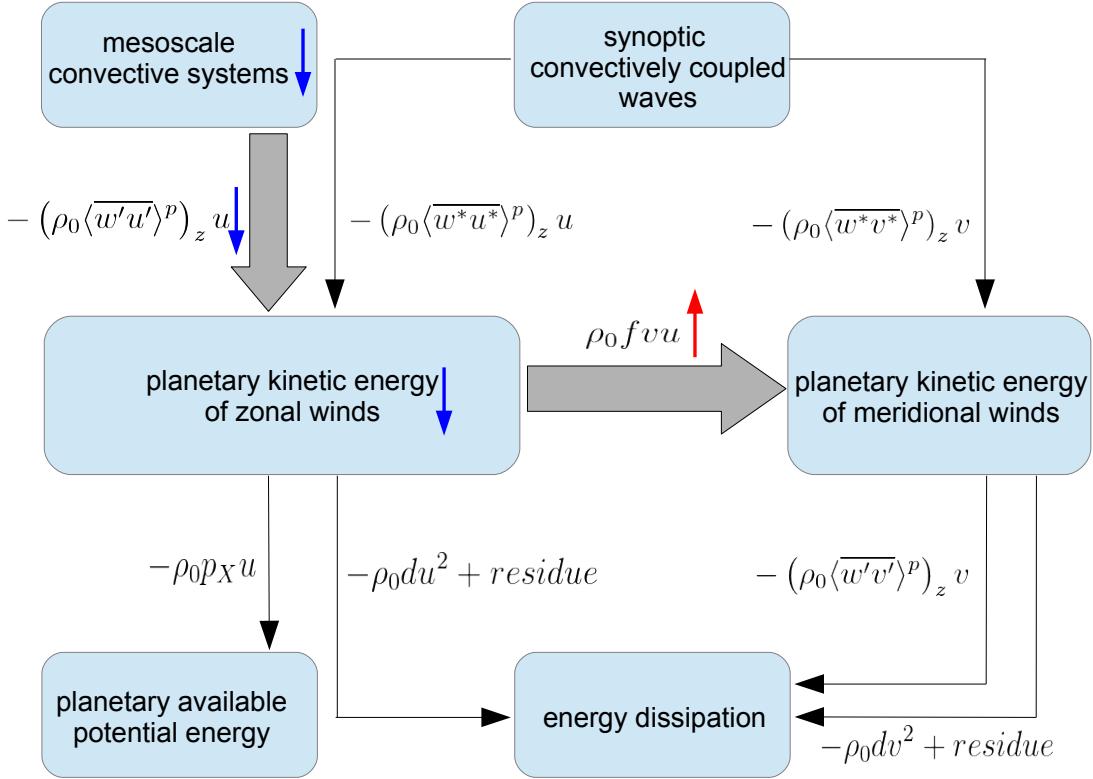


FIG. 8: Climatological-mean (zonal and vertical mean, and time-mean) total planetary-scale kinetic energy source and sink terms for (a) zonal winds, (b) meridional winds, based on the last 80-day model output in the weak rotation regime. The dimensional unit of all terms is $kgm^{-1}s^{-3}$. The y-axis limit in both panels are $2.35 \times 10^{-5} kg/m/s^3$.

(a) Planetary kinetic energy of zonal winds diminishes as rotation f increases



(b) Mesoscale convective systems diminishes as rotation f increases

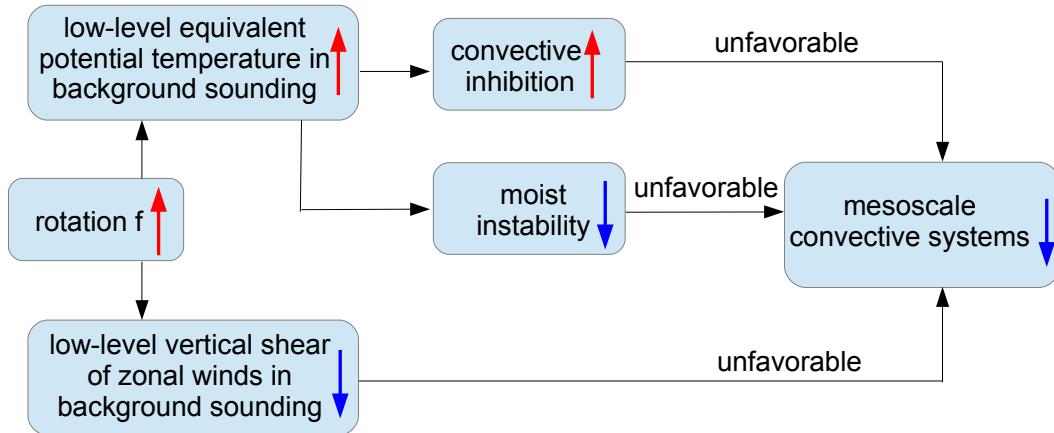


FIG. 9: Schematic diagram explaining why planetary-scale kinetic energy of zonal winds diminishes as the rotation f increases in the weak rotation regime. Panel (a) shows acceleration/deceleration effects in the planetary-scale kinetic energy budget of both zonal and meridional winds, where bold (thin) arrows indicate the dominant (secondary) energy source/sink terms. The red up (blue down) arrow represents increasing (decreasing) in magnitude. Overall, the diminishment of planetary kinetic energy of zonal winds is due to i) increasing deceleration term involving the Coriolis force, and ii) decreasing acceleration term involving eddy zonal momentum transfer from mesoscale fluctuations. Panel (b) attributes the diminishment of mesoscale convective systems to the increasing low-level equivalent potential temperature and decreasing low-level vertical shear in the background sounding as the rotation f increases.

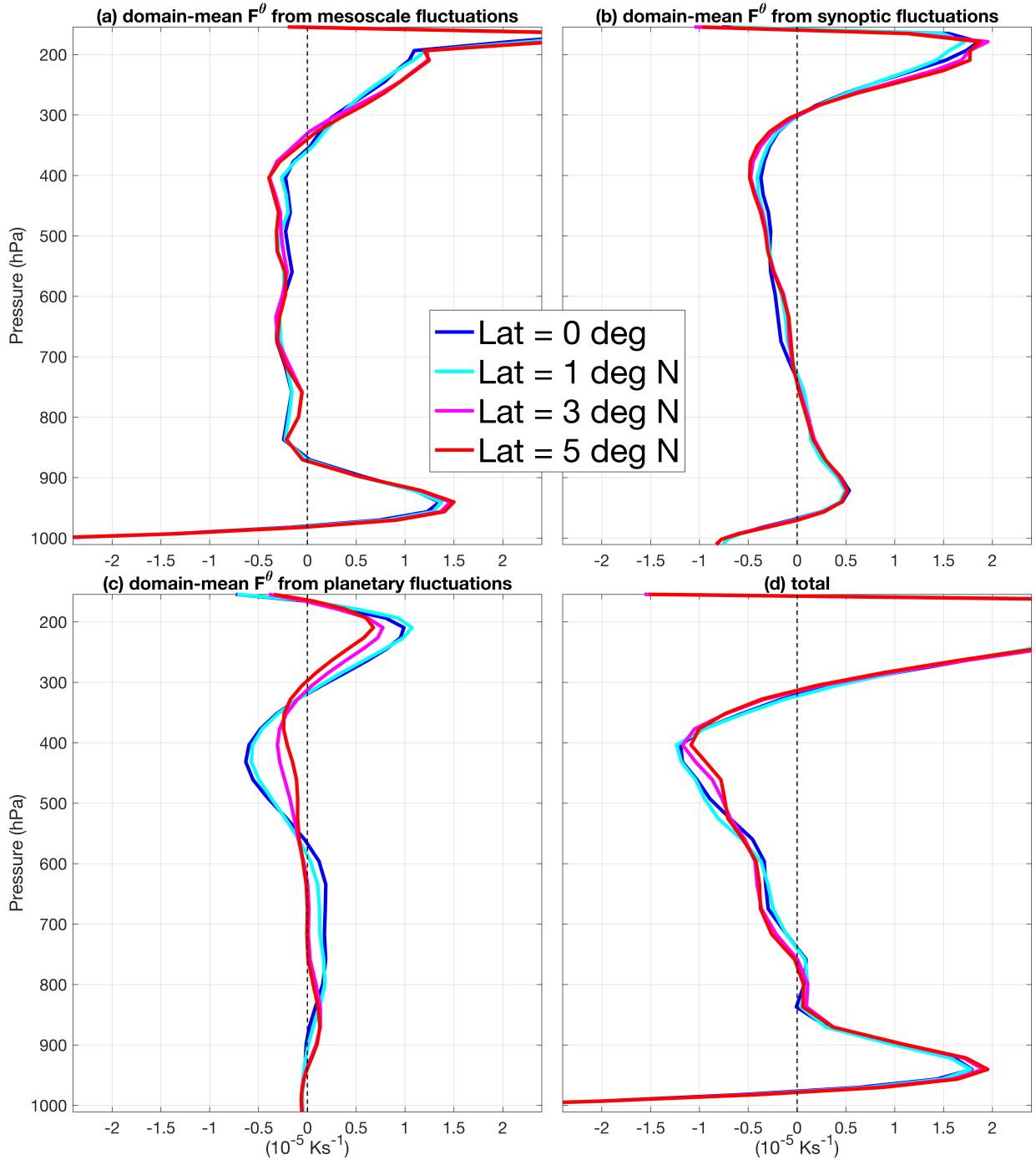


FIG. 10: Vertical profiles of climatological-mean (domain-mean and time-mean) eddy heat transfer from (a) mesoscale fluctuations, (b) synoptic fluctuations, (c) planetary fluctuations, and (d) total, based on the last 80-day model output in the weak rotation regime. The unit of eddy heat transfer is Ks^{-2} .

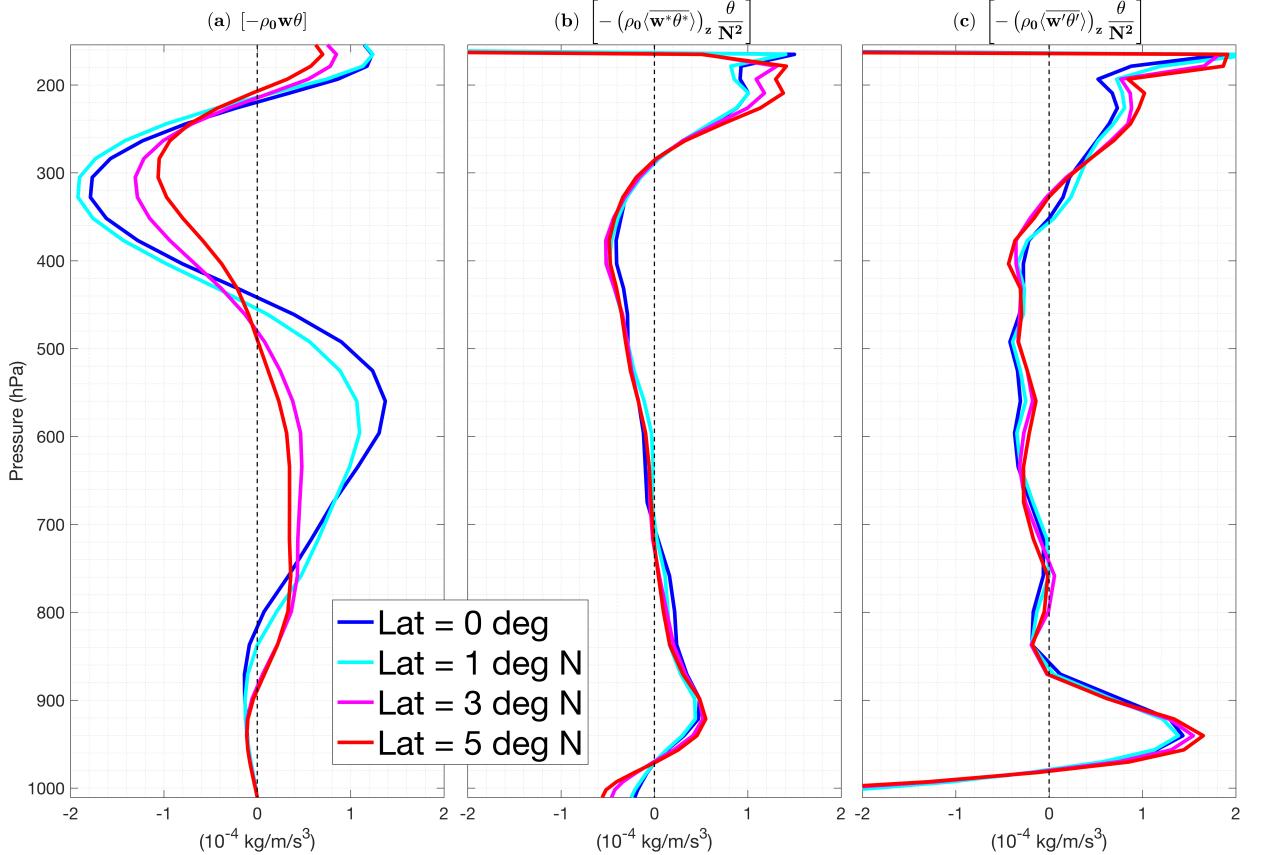


FIG. 11: Vertical profiles of climatological-mean (domain-mean and time-mean) available potential energy source and sink terms, based on the last 80-day model output in the weak rotation regime. Panel (a) shows the term involving energy transfer between kinetic energy and available potential energy. Panels (b-c) show available potential energy source and sinks terms involving eddy heat transfer from (b) synoptic fluctuations, (c) mesoscale fluctuations. Potential temperature is rescaled by a constant, $\tilde{\theta} = \frac{g}{\theta} \theta$. The dimensional unit of all terms is $\text{kg m}^{-1} \text{s}^{-3}$.

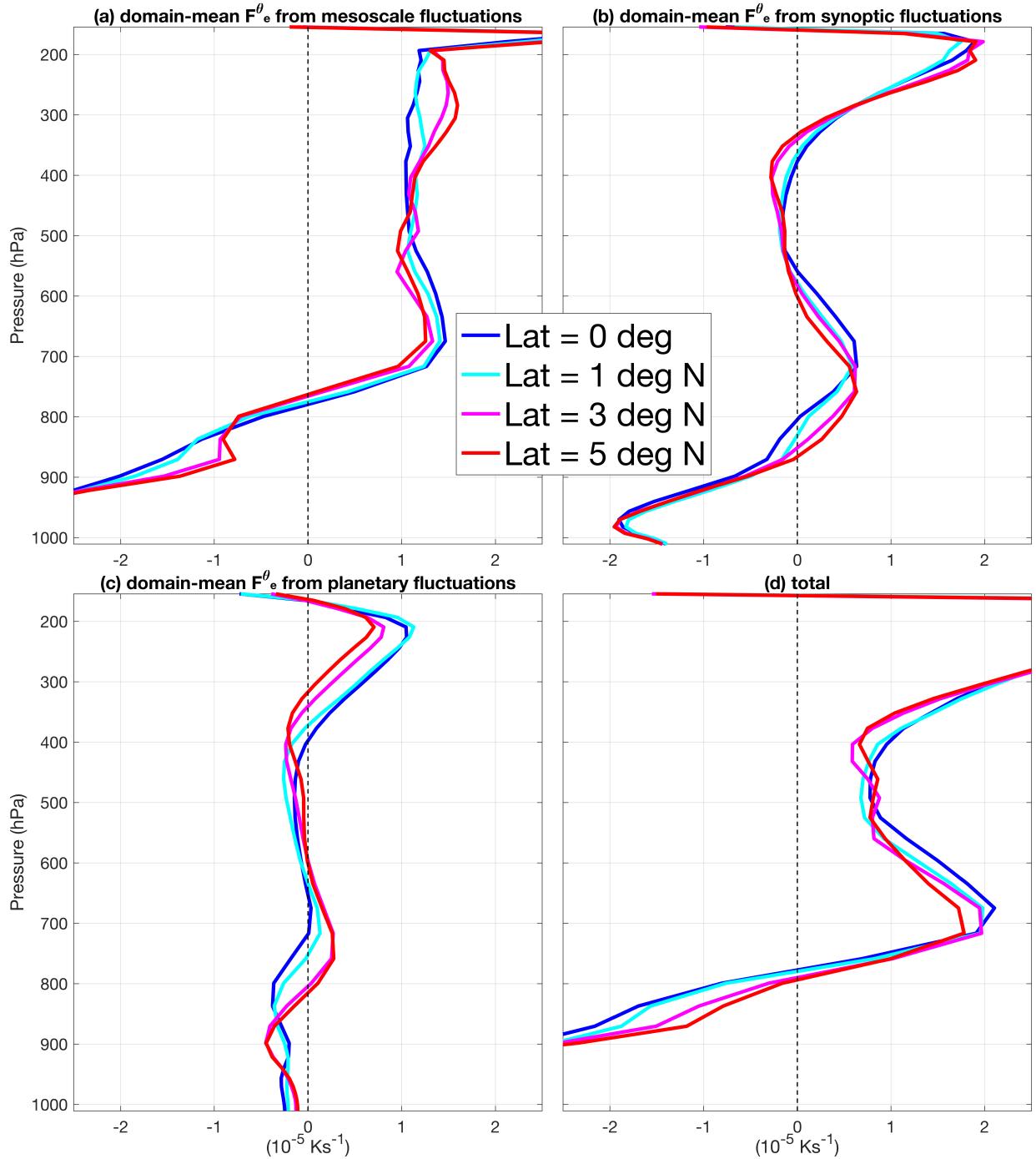


FIG. 12: Vertical profiles of climatological-mean (domain-mean and time-mean) eddy transfer of equivalent potential temperature from (a) mesoscale fluctuations, (b) synoptic fluctuations, (c) planetary fluctuations, and (d) total, based on the last 80-day model output in the weak rotation regime. The unit of eddy transfer of equivalent potential temperature is K/s .

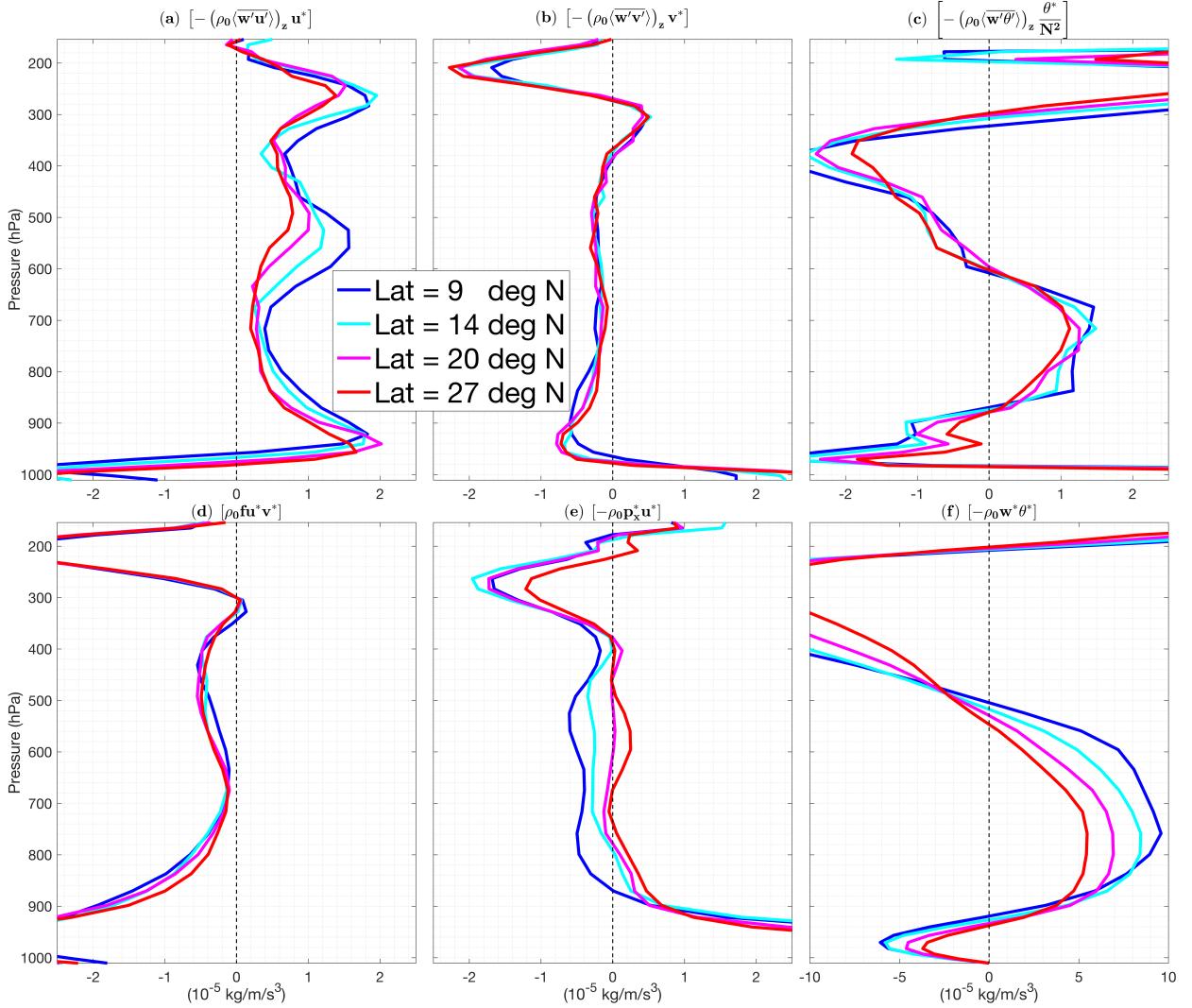


FIG. 13: Vertical profiles of climatological-mean (domain-mean and time-mean) synoptic-scale energy source and sink terms based on the last 80-day model output in the order-one rotation regime. Panels (a-d) show the terms involving (a) eddy zonal momentum transfer, (b) eddy meridional momentum transfer, (c) eddy heat transfer, (d) the Coriolis force. Panel (e-f) show the terms representing energy conversion between kinetic energy and available potential energy. The dimensional unit of all terms is $10^{-5} \text{kg m}^{-1} \text{s}^{-3}$.

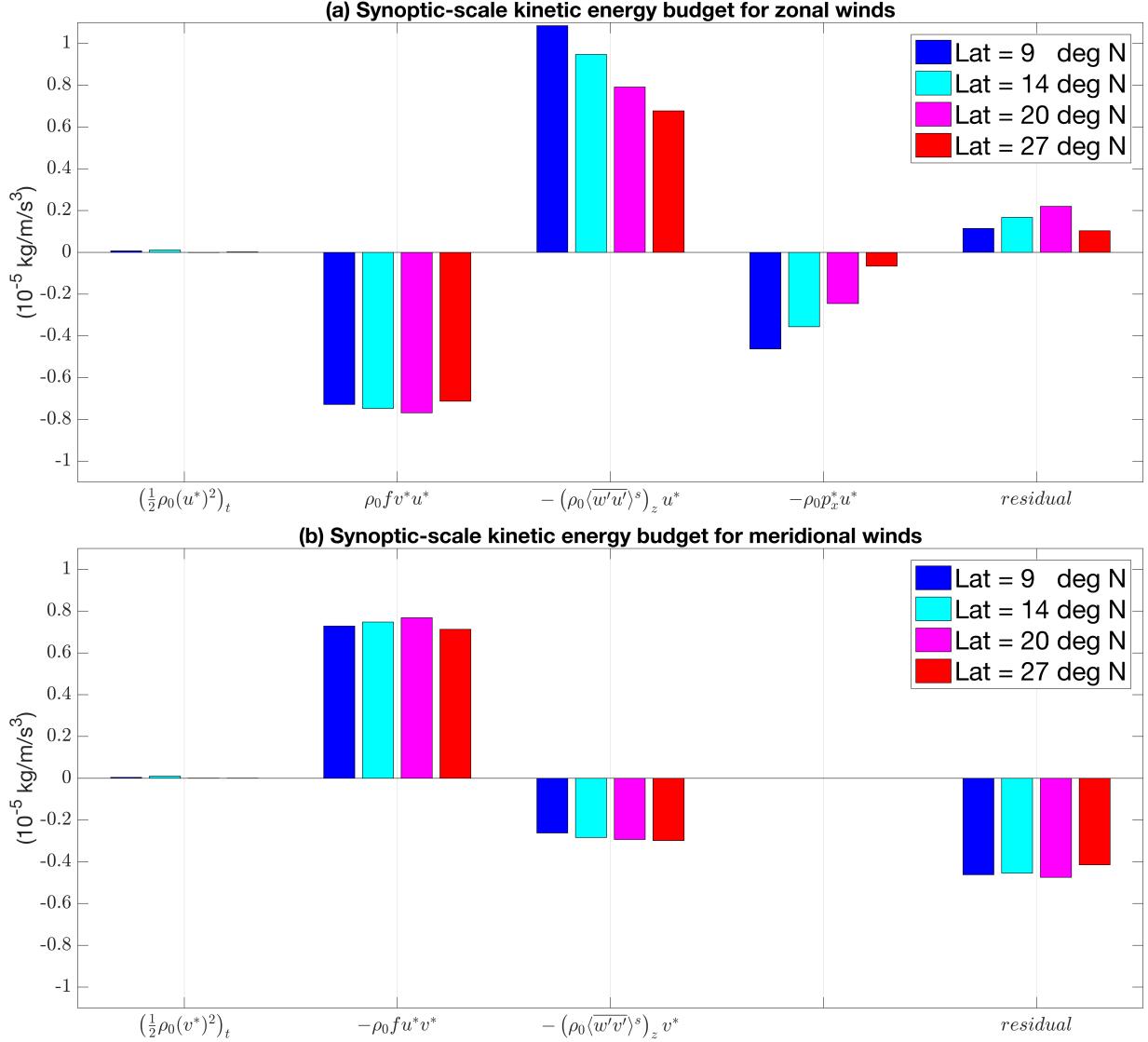


FIG. 14: Climatological-mean (zonal and vertical mean, and time-mean) total synoptic-scale kinetic energy source and sink terms for (a) zonal winds, (b) meridional winds, based on the last 80-day model output in the order-one rotation regime. The dimensional unit of all terms is $kgm^{-1}s^{-3}$. The y-axis limit in both panels are $1.1 \times 10^{-5} kg/m/s^3$.

Synoptic kinetic energy of zonal winds diminishes as rotation f increases

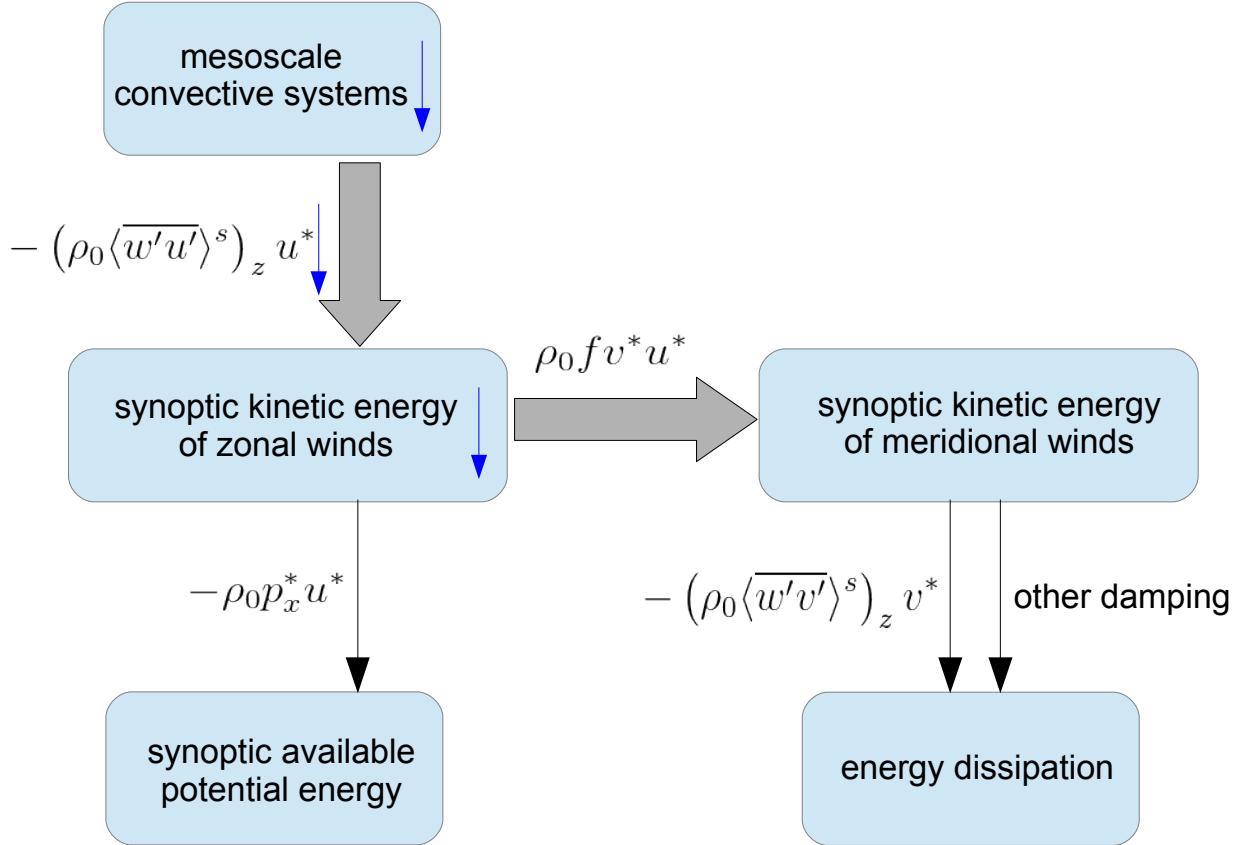


FIG. 15: Schematic diagram explaining the maintenance of synoptic organization of convection and its diminishment as the rotation further increases in the order-one rotation regime. This figure shows acceleration/deceleration effects in the synoptic-scale kinetic energy budget of both zonal and meridional winds, where bold (thin) arrows indicate the dominant (secondary) energy source/sink terms. The blue down arrow represents decreasing in magnitude. Overall, the diminishment of synoptic kinetic energy of zonal winds is due to decreasing acceleration term involving eddy zonal momentum transfer from mesoscale fluctuations. The explanation for the diminishment of mesoscale convective systems is the same as Fig.12, so it is not repeated here.

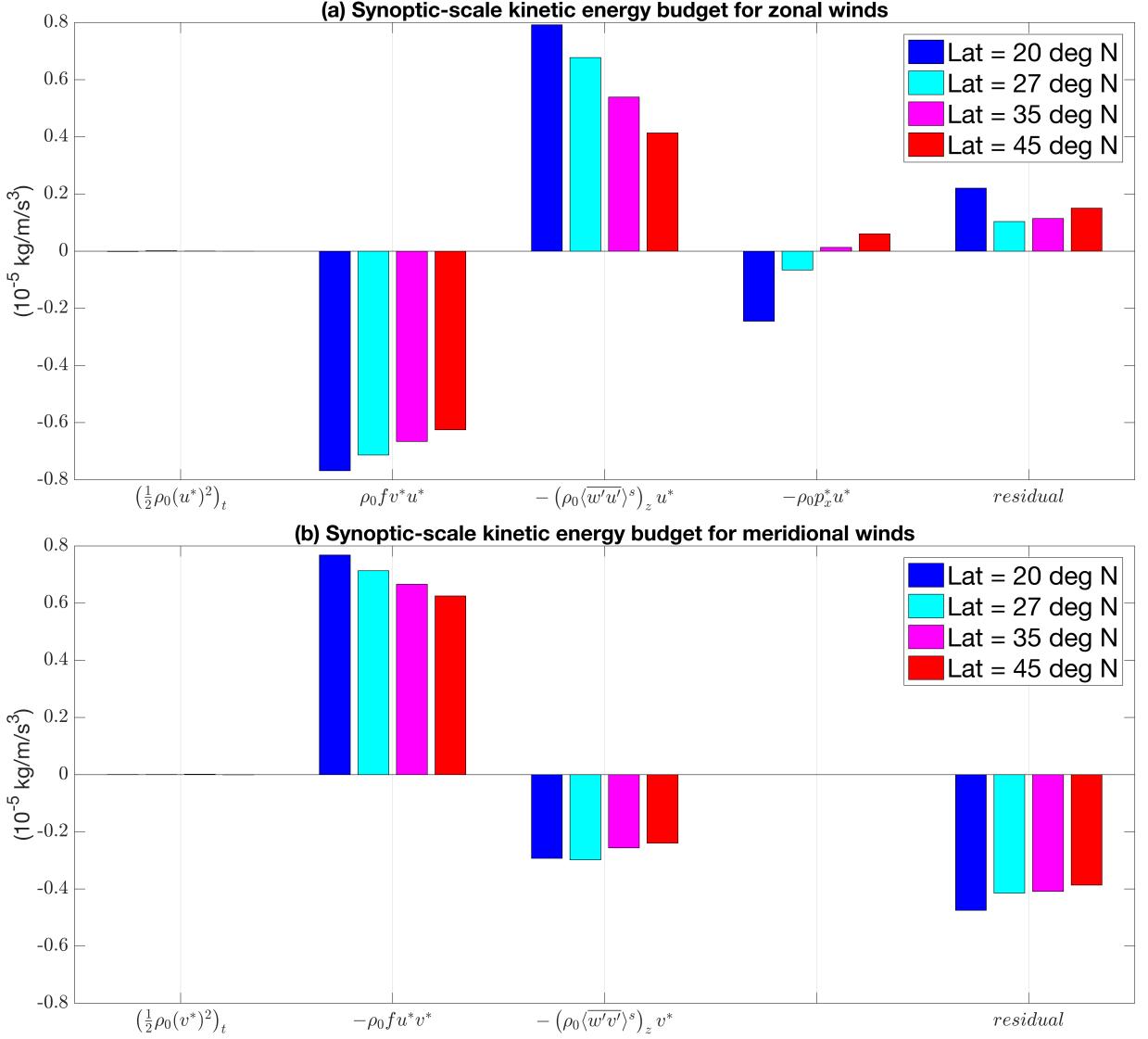


FIG. 16: Climatological-mean (zonal and vertical mean, and time-mean) total synoptic-scale kinetic energy source and sink terms for (a) zonal winds, (b) meridional winds, based on the last 80-day model output in the strong rotation regime. The dimensional unit of all terms is $\text{kgm}^{-1}\text{s}^{-3}$. The y-axis limit in both panels are $0.80 \times 10^{-5} \text{ kg/m/s}^3$.