

### Homework 3 / due October 3

1. Determine all groups of order 36.
2. Realize the dihedral group of order  $2n$  as a subgroup of a symmetric group.
3. Find all subgroups of the symmetric group  $\mathfrak{S}_4$  of order 8.
4. Assume that  $G$  is generated by two elements and that  $\exp(G) = 3$ , i.e., for every  $g \in G$ ,  $g^3 = 1$ . Show that  $G$  is finite.
5. Assume that  $2 \nmid n$  and that  $n \geq 3$ . Show that the permutations  $(123)$  and  $(123 \dots n)$  generate the alternating group  $\mathfrak{A}_n$ .