

Geometry Seminar  
April 1, 2008, Tuesday, 6:00 p.m.  
Room 613, Courant Institute  
251 Mercer Street, New York

## 20 years of EPT graphs: edge intersection graphs of paths in a tree

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### Abstract

Let  $P$  be a collection of nontrivial simple paths on a host tree  $T$ . The edge intersection graph of  $P$ , denoted by  $EPT(P)$ , has vertex set that corresponds to the members of  $P$ , where two vertices are joined by an edge if and only if the corresponding members of  $P$  share at least one common edge in  $T$ . An undirected graph  $G$  is called an *edge intersection graph of paths in a tree* if  $G = EPT(P)$  for some  $P$  and  $T$ . The  $EPT$  graphs can be useful in network applications. Scheduling undirected calls in a tree network or assigning wavelengths to virtual connections in an optical tree network are equivalent to coloring its  $EPT$  graph.

In this lecture, we will survey the mathematical and algorithmic results on  $EPT$  graphs and some of their generalizations. The class of  $EPT$  graphs was first investigated by Golumbic and Jamison in two papers appearing in 1985, and subsequently, further research has been carried out by a number of algorithmic graph theorists. On the algorithmic side, the recognition and coloring problems are  $NP$ -complete, whereas the maximum clique and maximum stable set problems are polynomially solvable. On the mathematical side, for example, it was shown 20 years ago, that the  $EPT$  graphs restricted to host trees of vertex degree 3 are precisely the chordal  $EPT$  graphs. A new analogous result by Golumbic, Lipshteyn and Stern is that weakly chordal  $EPT$  graphs are precisely the  $EPT$  graphs with host tree restricted to degree 4. A complete hierarchy of related graph classes will also be presented, including the  $k$ - $EPT$  graphs in which paths must share at least  $k$  edges of the tree in order to generate an edge in the  $k$ - $EPT$  graph.