

**Erratum:**  
**On the spectra of**  
**randomly perturbed expanding maps**

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The authors wish to point out an error in Sublemma 6 in Section 5 of [1]. The claims in Theorems 3 and 3' have been revised accordingly; a correct version is given below. Other results in [1] are not affected.

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**i) Revised statement of results in Section 5.C.**

Section 5 of [1] is about piecewise  $C^2$  expanding mixing maps  $f$  of the interval. The number  $\Theta$  below refers to  $\Theta = \lim_{n \rightarrow \infty} \sup(1/|(f^n)'|^{1/n})$ . These maps are randomly perturbed by taking convolution with a kernel  $\theta_\epsilon$ , and the resulting Markov chain is denoted  $\mathcal{X}^\epsilon$ . The precise statements of Theorems 3 and 3' should read as follows:

**Theorem 3.** *Let  $f : I \rightarrow I$  be as described in Section 5.A of [1], with a unique absolutely continuous invariant probability measure  $\mu_0 = \rho_0 dm$ , and let  $\mathcal{X}^\epsilon$  be a small random perturbation of  $f$  of the type described in Section 5.B with invariant probability measure  $\rho_\epsilon dm$ . We assume also that  $f$  has no periodic turning points. Then*

- (1) *The dynamical system  $(f, \mu_0)$  is stochastically stable under  $\mathcal{X}^\epsilon$  in  $L^1(dm)$ , i.e.,  $|\rho_\epsilon - \rho_0|_1$  tends to 0 as  $\epsilon \rightarrow 0$ .*

*Let  $\tau_0 < 1$  and  $\tau_\epsilon < 1$  be the rates of decay of correlations for  $f$  and  $\mathcal{X}^\epsilon$  respectively for test functions in  $BV$ . Then:*

- (2)  $\limsup_{\epsilon \rightarrow 0} \tau_\epsilon \leq \sqrt{\tau_0}$ .

**Theorem 3'.** *Let  $f$  and  $\mathcal{X}^\epsilon$  be as in Theorem 3, except that we do not require that  $f$  has no periodic turning points. Then*

- (1)  $|\rho_\epsilon - \rho_0|_1$  tends to 0 as  $\epsilon \rightarrow 0$  if  $2 < 1/\tau_0 \leq 1/\Theta$ ;
- (2)  $\limsup_{\epsilon \rightarrow 0} \tau_\epsilon \leq \sqrt{2\tau_0}$ .

*If  $\theta_\epsilon$  is symmetric, the factor "2" in both (1) and (2) may be replaced by "3/2".*

Section 5.D is unchanged.

## ii) Revised version of Section 5.E.

We follow the notation introduced at the beginning of 5.E, except that we consider only the situation where

$$\Sigma_0 = \{1\} \quad \text{and} \quad \Sigma_{1,0} = \emptyset.$$

That is to say, the reader should read 5.E with  $\kappa_0 = 1$ ,  $\kappa_{11} = \kappa_1 = \tau_0$ , etc.

Sublemma 6, which is problematic in [1], is valid in this more limited setting because  $\pi_0\varphi = \rho_0 \cdot \int \varphi dm$ . Lemmas 1' and 3', which use Sublemma 6, are also correct under the present assumptions. We take this opportunity to add " $X_0^\epsilon \rightarrow X_0$ ", which had been inadvertently left out in [1], to the conclusion of Lemma 3'.

To prove Theorem 3, one applies Lemmas 9, 1' and 3' with  $\kappa$  close to (and slightly bigger than)  $\sqrt{\tau_0}$ . To prove Theorem 3', take  $\kappa$  close to  $\sqrt{\tau_0/2}$  (or  $\sqrt{\tau_0/(3/2)}$  if  $\theta_\epsilon$  is symmetric).

## REFERENCES

1. V. Baladi and L.-S. Young, *On the spectra of randomly perturbed expanding maps*, Comm. Math. Phys. **156** (1993), 355-385.

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