

## Course description.

**Week 1.** Statistics and data. Descriptive Statistics. Mean, Median, Quartiles, Percentiles, Variance, Moments, Histograms, Order Statistics, tables etc. Raw and processed data, regression, correlation etc.

**Week 2.** Analysis of data, inferences from data, ambiguities and uncertainties. Level of ambiguity. How strong is the evidence? Indicative, convincing, overwhelming. Quantification. Examples. Prior knowledge. Errors in measurement. Tolerances.

**Week 3.** Probability as a tool to quantify uncertainty. Trial, outcomes, events, probabilities and probability distributions. Repeated trials, independence. Induced distributions. Conditional probability and Bayes' rule.

**Week 4.** Calculation of probabilities and some standard distributions. Binomial, Poisson, Geometric, Uniform, Negative Binomial. Moments, generating functions. Poisson as a limit of Binomial.

### QUIZ.

**Week 5.** Random variables, their distributions, expectations, sums of independent random variables.

**Week 6.** Laws of large numbers. Basis for reliability of inference based on large samples. Notion of orthogonality of distributions.

**Week 7.** Continuous distributions, Distribution functions, densities. Approximations to discrete distributions. Some standard continuous distributions.

### MID TERM EXAMINATION.

**Week 8.** Moments, bivariate distributions, correlations, conditional distributions. Normal distributions.

**Week 9.** Statistical inference. Testing simple null hypothesis against a simple alternative. Critical Region. Size or level of a test. Type I and Type II errors. Power. Trade-offs. Selection of the critical region. Neyman-Pearson lemma. Bayesian approach. Priors and posteriors.

**Week 10.** Some examples of simple tests. Composite alternatives. UMP tests. One sided and two sided tests. Testing for means, variances in a normal population.

**Week 11.** Standard tests:  $z$ -score. " $t$ " and " $F$ " tests. Small sample and large sample tests.

### QUIZ.

**Week 12.** Estimation. Method of moments. Unbiased Estimators. Variances. Cramer-Rao inequality. Consistency. Examples.

**Week 13.** Maximum likelihood estimators. Asymptotic properties. Examples.

**Week 14.** Testing for correlations and regression coefficients. Non-parametric inference.  
Run test.

**Weak 15.** Revision.

**FINALS.**